

CS61A Lecture 40

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Announcements



- ☐ HW12 due tonight
- □ HW13 out
- ☐ Scheme project, contest due Monday

Logic Language Review



Expressions begin with query or fact followed by relations

Expressions and their relations are Scheme lists

logic> (fact (parent eisenhower fillmore)) logic> (fact (parent fillmore abraham))

logic> (fact (parent abraham clinton))

logic (fact (ancestor ?a ?y) (parent ?a ?y))
logic (fact (ancestor ?a ?y) (parent ?a ?z) (ancestor ?z ?y))

logic> (query (ancestor ?who abraham))

Success! who: fillmore who: eisenhower

If a fact has more than one relation, the first is the conclusion, and it is satisfied if the remaining relations, the hypotheses, are satisfied

If a query has more than one relation, all must be satisfied

The interpreter lists all bindings that it can find to satisfy the query

Hierarchical Facts



Relations can contain relations in addition to atoms

logic> (fact (dog (name abraham) (color white))) logic> (fact (dog (name barack) (color tan)))
logic> (fact (dog (name clinton) (color white)))

logic> (fact (dog (name delano) (color white))) logic> (fact (dog (name eisenhower) (color tan)))
logic> (fact (dog (name fillmore) (color brown)))

logic> (fact (dog (name grover) (color tan)))
logic> (fact (dog (name herbert) (color brown)))

Variables can refer to atoms or relations

logic> (query (dog (name clinton) (color ?color))) Success! color: white

logic> (query (dog (name clinton) ?info))

info: (color white)

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Example: Combining Multiple Data Sources



Which dogs have an ancestor of the same color?

logic> (query (dog (name ?name) (color ?color)) (ancestor ?ancestor ?name)

(dog (name ?ancestor) (color ?color)))

Success!

name: barack color: tan ancestor: eisenhower name: clinton color: white ancestor: abraham color: tan ancestor: eisenhower name: grover name: herbert color: brown ancestor: fillmore

Example: Appending Lists

Two lists append to form a third list if:

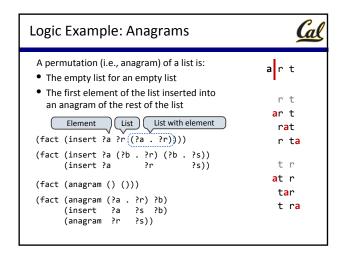
• The first list is empty and the second and third are the same

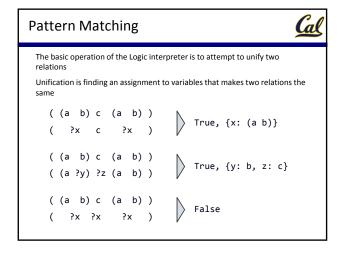
() (a b c) (a b c)

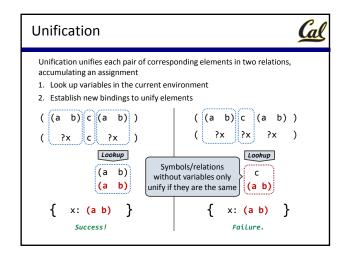
- · Both of the following hold:
- List 1 and 3 have the same first element
- The rest of list 1 and all of list 2 append to form the rest of list 3

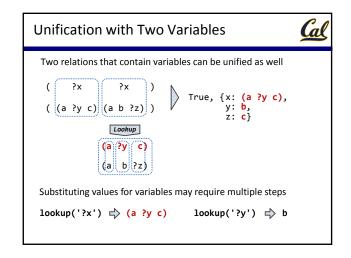
(a b c) (d e f) (a b c d e f)

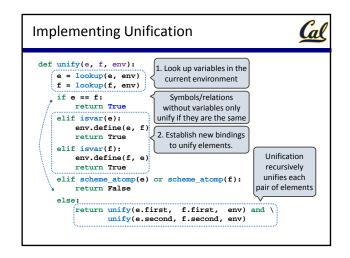
logic> (fact (append-to-form () ?x ?x)) logic> (fact (append-to-form (?a . ?r) ?y (?a . ?z)) (append-to-form ?r ?y ?z))











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Searching for Proofs
 The Logic interpreter searches
                                   (fact (app () ?x ?x))
 the space of facts to find
                                  (fact (app (?a . ?r) ?y (?a . ?z))
(app ?r ?y ?z )
 unifying facts and an env that
 prove the query to be true
                                   (query (app ?left (c d) (e b c d)))
 (app ?left (c d) (e b c d))
     {a: e, y: (c d), z: (b c d), left: (?a . ?r)} ←
      (app (?a . ?r) ?y (?a . ?z))
         conclusion <- hypothesis
      (app ?r (c d) (b c d)))
         →{a2: b, y2: (c d), z2: (c d), r: (?a2 . ?r2)}
          (app (?a2 . ?r2) ?y2 (?a2 . ?z2)) ≼
                                               Variables are local to
               conclusion <- hypothesis</pre>
                                                 facts and queries
          (app ?r2 (c d) (c d))
                -{r2: (), x: (c d)}
                (app () ?x ?x)
```

Underspecified Queries



Search for possible unification



The space of facts is searched exhaustively, starting from the query and following a *depth-first* exploration order

A possible proof is explored exhaustively before another one is considered

Some good ideas:

- Limiting depth of the search avoids infinite loops
- Each time a fact is used, its variables are renamed
- Bindings are stored in separate frames to allow backtracking

Implementing Search



An Evaluator in Logic

