

CS61A Lecture 34

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Announcements



□ HW10 deadline extended to 11:59pm Thursday

☐ Scheme project out







The user interface to many programming languages is an interactive loop, which

Reads an expression from the user,



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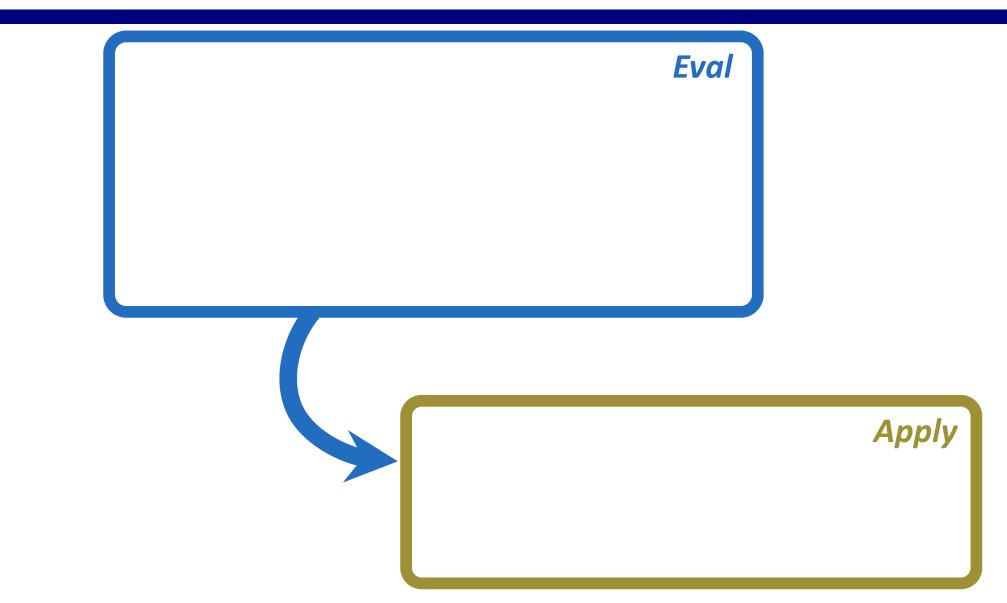
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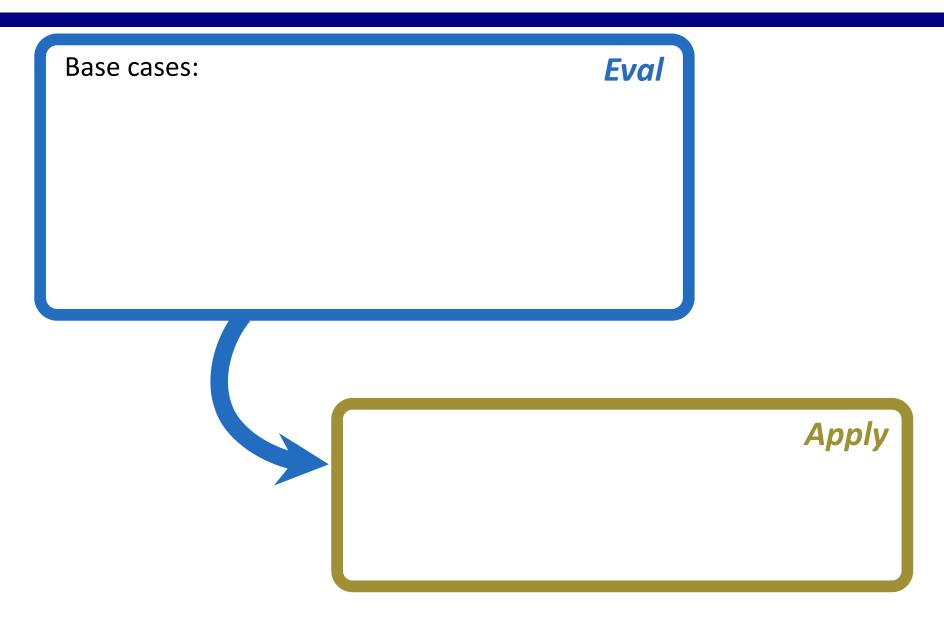
A well-designed REPL should not crash on any input!



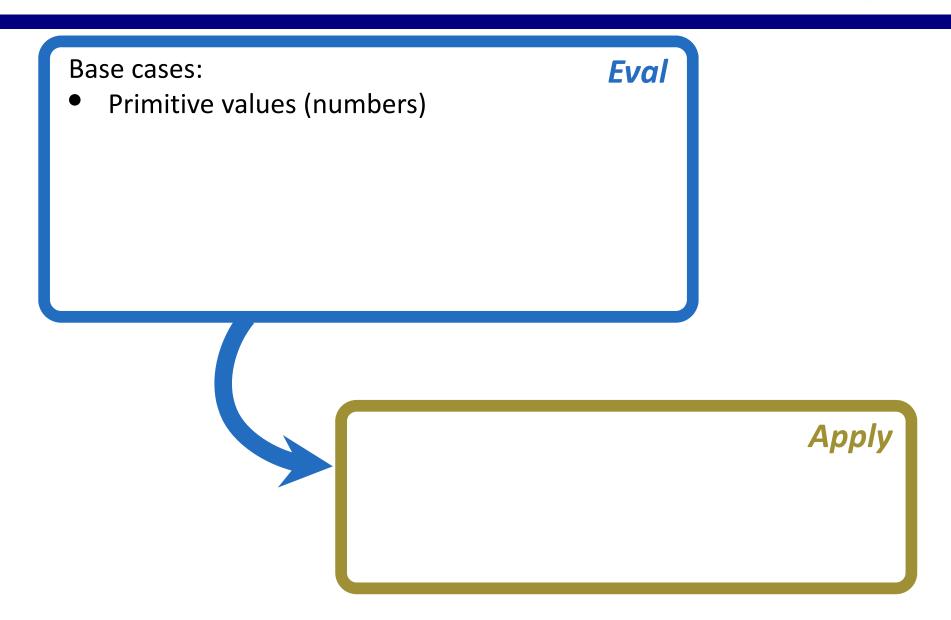




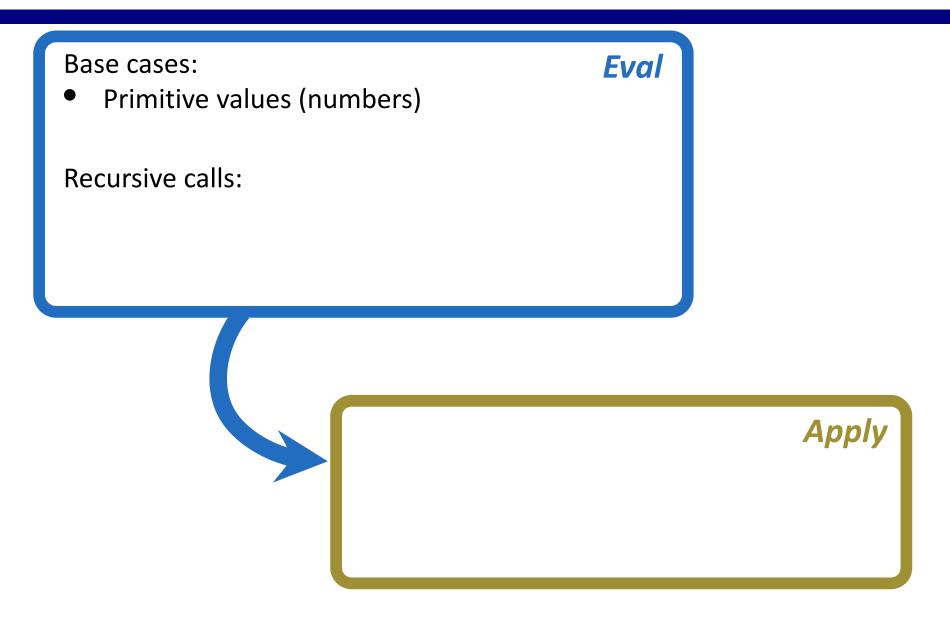




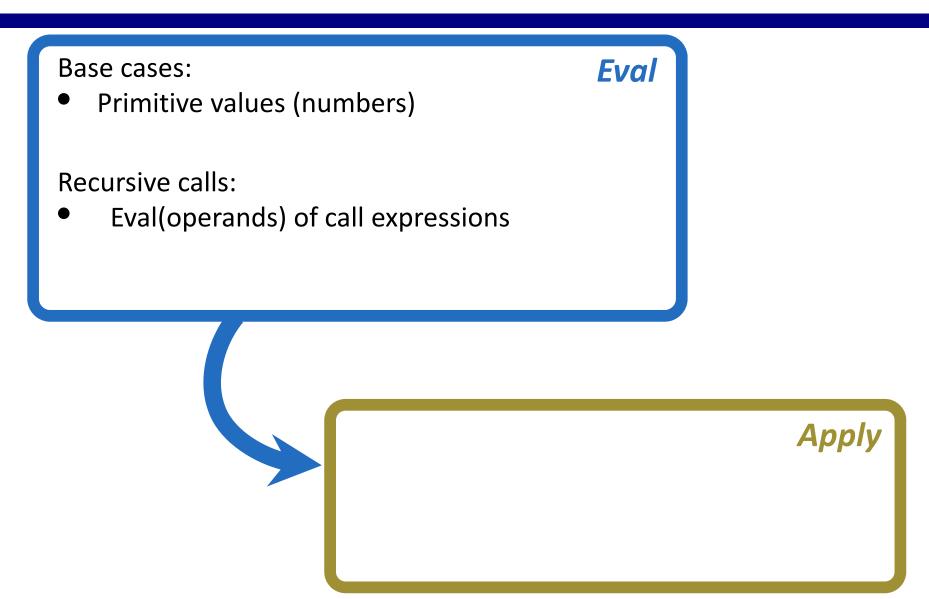














Base cases:

Primitive values (numbers)

Recursive calls:

- Eval(operands) of call expressions
- Apply(operator, arguments)

Apply

Eval



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Built-in primitive procedures

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- Eval(sub-expressions) of special forms

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Eval(body) of user-defined proc's



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Requires an environment for name lookup

Creates new environments when applying user-defined procedures

Base cases:

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Eval(body) of user-defined proc's

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The **scheme_eval** function dispatches on expression form:

Symbols are bound to values in the current environment



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(if consequent> <alternative>)
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```
(if  <consequent> <alternative>)
  (lambda (<formal-parameters>) <body>)
```



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```
(if  <consequent> <alternative>)
  (lambda (<formal-parameters>) <body>)
        (define <name> <expression>)
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```
Special forms are identified by the first list element (if (consequent < consequent < conse
```



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```
< <consequent> <alternative>)
                                                        Anything not
             (lambda (<formal-parameters>) <body>)
  Special
                                                         a known
 forms are
                  (define <name> <expression>)
                                                        special form
identified by
                                                          is a call
           (<operator> <operand 0> ... <operand k>
the first list
                                                         expression
 element
(define (f s) (if (null? s) '(3) (cons (car s) (f (cdr s)))))
                          (f (list 1 2))
```





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- And and or: (and $\langle e_1 \rangle$... $\langle e_n \rangle$), (or $\langle e_1 \rangle$... $\langle e_n \rangle$)



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The value of an **if** expression is the value of a sub-expression.

- Evaluate the predicate.
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- Evaluate that sub-expression in place of the whole expression.



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scheme_eval





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The **scheme_read** parser converts shorthand to a combination







```
(lambda (<formal-parameters>) <body>)
```



```
(lambda (<formal-parameters>) <body>)
    (lambda (x) (* x x))
```



```
(lambda (<formal-parameters>) <body>)
              (lambda (x) (* x x))
class LambdaProcedure(object):
   def __init__(self, formals, body, env):
       self.formals = formals
       self.body = body
       self.env = env
```



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(lambda (<formal-parameters>) <body>)
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                                 A scheme expression
        self.body = body
                                A Frame instance
        self.env = env
```





A frame represents an environment by having a parent frame



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Frames are Python instances with methods lookup and define



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In Project 4, **Frames** do not hold return values



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Frames and Environments



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Define expressions bind a symbol to a value in the first frame of the current environment



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(define <name> <expression>)
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Procedure definition is a combination of define and lambda



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```



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```
(define <name> <expression>)
```

Evaluate the **<expression>**

Bind <name> to the result (define method of the current Frame)

```
(define x 2)
```

Procedure definition is a combination of define and lambda

```
(define (<name> <formal parameters>) <body>)
(define <name> (lambda (<formal parameters>) <body>))
```





Create a new frame in which formal parameters are bound to argument values, whose parent is the **env** of the procedure



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```

```
g: Global frame

f LambdaProcedure instance [parent=g]
```



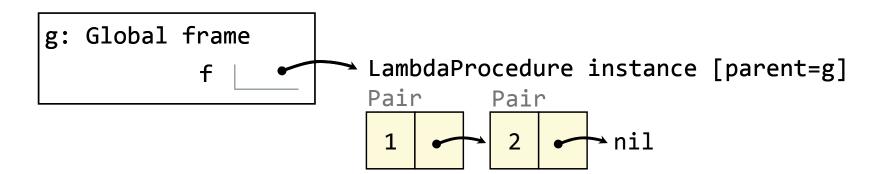
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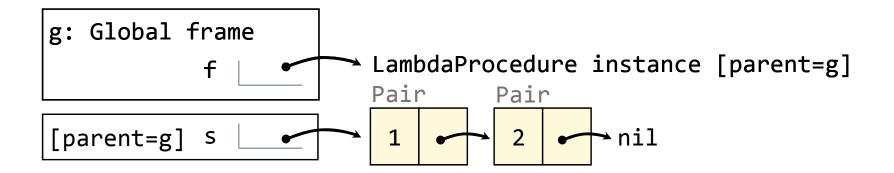


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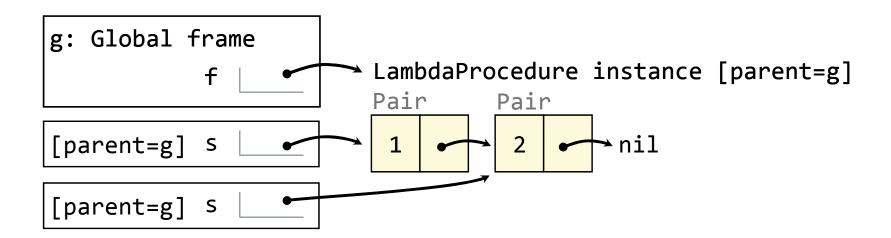


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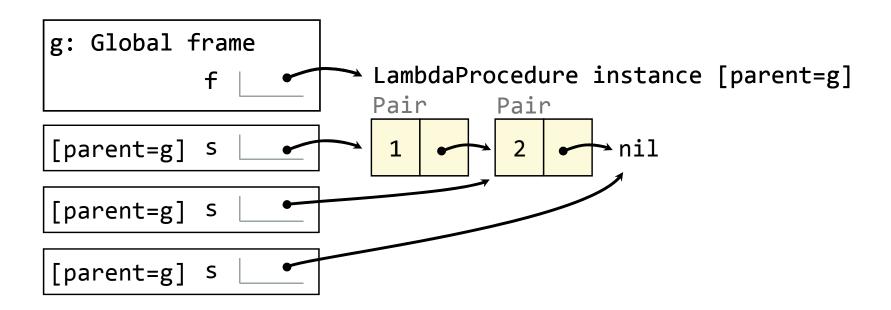


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Eval/Apply in Lisp 1.5



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```
apply[fn;x;a] =
      [atom[fn] \rightarrow [eq[fn;CAR] \rightarrow caar[x];
                     eq[fn;CDR] \rightarrow cdar[x];
                     eq[fn;CONS] \rightarrow cons[car[x];cadr[x]];
                     eq[fn;ATOM] \rightarrow atom[car[x]];
                     eq[fn; EQ] \rightarrow eq[car[x]; cadr[x]];
                     T \rightarrow apply[eval[fn;a];x;a]];
      eq[car[fn]; LAMBDA] \rightarrow eval[caddr[fn]; pairlis[cadr[fn]; x; a]];
      eq[car[fn]; LABEL] - apply[caddr[fn]; x; cons[cons[cadr[fn];
                                                      caddr[fn]];a]]]
eval[e;a] = [atom[e] - cdr[assoc[e;a]];
      atom[car[e]]-
                 [eq[car[e],QUOTE] \rightarrow cadr[e];
                 eq[car[e];COND] - evcon[cdr[e];a];
                 T - apply[car[e];evlis[cdr[e];a];a]];
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```





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(define f (lambda (x) (+ x y)))
```



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```
(define f (lambda (x) (+ x y)))
(define g (lambda (x y) (f (+ x x))))
```



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Lexical scope: The parent of a frame is the environment in which a procedure was *defined*

Dynamic scope: The parent of a frame is the environment in which a procedure was *called*

Lexical scope: The parent for **£**'s frame is the global frame



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Dynamic scope: The parent for £'s frame is g's frame



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Error: unknown identifier: y

Dynamic scope: The parent for **f**'s frame is **g**'s frame



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Lexical scope: The parent of a frame is the environment in which a procedure was *defined*

Dynamic scope: The parent of a frame is the environment in which a

```
Special form to create dynamically scoped procedures

(define f (lambda (x) (+ x y)))

(define g (lambda (x y) (f (+ x x))))
```

(q 3 7)

Lexical scope: The parent for £'s frame is the global frame

Error: unknown identifier: y

Dynamic scope: The parent for £'s frame is g's frame