

# CS61A Lecture 13

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### Announcements



- ☐ HW4 due today at 11:59pm
- ☐ Hog contest deadline on Friday
  - □ Completely optional, opportunity for extra credit
  - ☐ See website for details

## Converting Recursion to Iteration

return total



Can be tricky! Iteration is a special case of recursion Idea: Figure out what state must be maintained by the function

```
def summation(n, term):
    if n = 0:
        return(0) Initial value
    return (summation(n - 1, term)) + (term(n))
        What's summed so far? How to get each incremental piece

def summation iter(n, term):
    (total) = (0)
    while (n > 0)
    total, n = total + (term(n), n - 1)
```

# Converting Iteration to Recursion



More formulaic: Iteration is a special case of recursion Idea: The state of iteration can be passed as parameters

```
def fib iter(n):
    if n == 0:
                   Local names become...
       return 0
   (fib_n, fib_n_1, k)= 1, 0, 1
    while k < n:
        fib_n, fib_n_1 = fib_n + fib_n_1, fib_n
        k = k + 1
   return fib_n
def fib_rec(n, fib_n, fib_n_1, k):
    if n == 0:
                                Parameters in a
       return 0
                                recursive function
    if k >= n:
        return fib_n
    return fib_rec(n, fib_n + fib_n_1, fib_n, k + 1)
```

### **Mutual Recursion**



Mutual recursion is when the recursive process is split across multiple functions



Decorating a recursive function generally results in mutual recursion

@trace1
def factorial(n):
 if n == 0:
 return 1
 return n \* factorial(n-1)
Example: http://goo.gt/4LZZy

### Currying

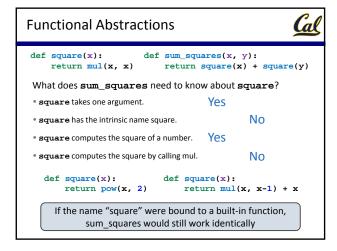


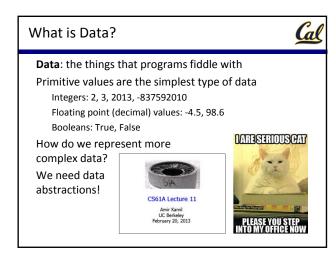
We have used higher-order functions to produce a function to add a constant to its argument  $\,$ 

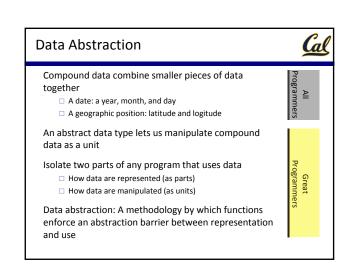
What if we wanted to do the same for multiplication?

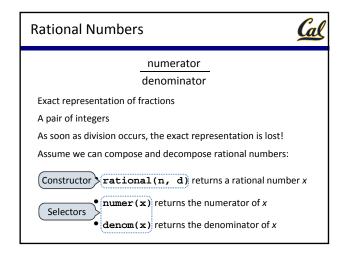
How can we do this in general without repeating ourselves?

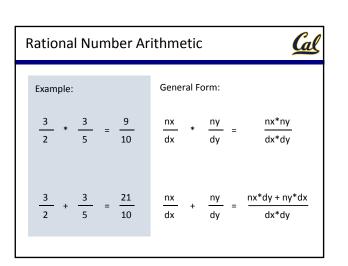
#### Cal Currying First, identify common structure. Then define a function that generalizes the procedure. def curry2(f): def make adder(n): def outer(n): def adder(k): def inner(k): return f(n, k) return add(n, k) return inner return adder return outer >>> make\_adder(2)(3) >>> curry2(mul)(2)(3) >>> add(2, 3) >>> mul(2, 3) This process of converting a multi-argument function to consecutive single-argument functions is called currying.











```
Tuples
   >>> pair = (1, 2) >>> pair
                                       A tuple literal:
                                       Comma-separated expression
   (1, 2)
   >>> x, y = pair
                                        "Unpacking" a tuple
   >>> x
   1
   >>> y
                                        Element selection
   >>> pair[0]
   >>> pair[1]
   >>> from operator import getitem
>>> getitem(pair, 0)
   >>> getitem(pair, 1)
                                 More tuples next lecture
```

```
Representing Rational Numbers

def rational(n, d):
    """Construct a rational number x that represents n/d."""
    return (n, d) Construct a tuple

from operator import getitem

def numer(x):
    """Return the numerator of rational number x."""
    return getitem(x, 0)

def denom(x):
    """Return the denominator of rational number x."""
    return getitem(x, 1) Select from a tuple
```