ITERATORS, GENERATORS, AND STREAMS 11

1 Introduction

Infinite sequences frequently arise in computer science. For example, the sequence of all natural numbers is an infinite sequence, because there is no "last" natural number. However, it is impossible to physically store an infinite amount of data. How do we get around this?

In this section, we will learn about iterators, generators, and streams – each of these constructs is designed to represent infinite sequences in a finite amount of memory.

2 Iterators

An *iterator* is an object that represents a sequence of values. Here is an example of a class that implements Python's iterator interface. This iterator calculates all of the natural numbers one-by-one, starting from zero:

```
class Naturals():
    def __init__(self):
        self.current = 0
    def __next__(self):
        result = self.current
        self.current += 1
        return result
    def __iter__(self):
        return self
```

There are two components of Python's iterator interface: the `__next__` method, and the `__iter__` method.

2.1 `__next__`

The `__next__` method does two things:

1. calculates the next value

2. checks if it has any values left to compute

To return the next value in the sequence, the iterator does some computation defined in the `__next__` method.

When there are no more values left to compute, the `__next__` method must raise a type of exception called `StopIteration`. This signals the end of the sequence.

Note: the `__next__` method defined above does NOT raise any `StopIteration` exceptions. Why? Because there are always more values left to compute! Remember, there is no "last natural number", so there is technically no "end of the sequence." However, if you wanted to define a *finite* iterator, then you would raise a `StopIteration` after returning the final value.

2.2 `__iter__`

The purpose of the `__iter__` method is to return an iterator object. **By definition**, an iterator object is an object that has implemented both the `__next__` and `__iter__` methods.

This has an interesting consequence. If a class implements both a `__next__` method and a `__iter__` method, its `__iter__` method can just return `self` (like in the example). Since the class implements both `__next__` and `__iter__`, it is technically an iterator object, so its `__iter__` method can just return itself.

2.3 Implementation

When defining an iterator object, you should always keep track of how much of the sequence has already been computed. In the above example, we use an instance variable `self.current` to keep track.

Iterator objects maintain state. Successive calls to `__next__` will most likely output different values each time, so `__next__` is considered *non-pure*.

How do we call `__next__` and `__iter__`? Python has built-in functions called `next` and `iter` for this. Calling `next(some_iterator)` will then cause Python to implicitly call `some_iterator`'s `__next__` method. Calling `iter(some_iterator)` will make a similar implicit call to `some_iterator`'s `__iter__` method.

For example, this is how we would use the `Naturals` iterator:

```
>>> nats = Naturals()
>>> nats_iter = iter(nats)
>>> next(nats_iter)
0
>>> next(nats_iter)
1
>>> next(nats_iter)
2
```

However, we don't really need to call `iter` on `nats`. Why not?

One other note: you can use iterator objects in `for` loops. In other words, any object that satisfies the iterator interface can be iterated over:

```
>>> nats = Naturals()
>>> for n in nats:
        print(n)
0
1
2
...  # Forever!
```

This works because the Python `for` loop implicitly calls the `__iter__` method of the object being iterated over, and repeatedly calls `next` on it. In other words, the above interaction is (basically) equivalent to:

```
nats_iter = iter(nats)
is_done = False
while not is_done:
    try:
        val = next(nats_iter)
        print(val)
    except StopIteration:
        is_done = True
```

2.4 Questions

1. Define an iterator whose *i*-th element is the result of combining the *i*-th elements of two input iterables using some binary operator, also given as input. The resulting iterator should have a size equal to the size of the shorter of its two input iterators.

   ```
   >>> from operator import add
   >>> evens = Iter_Combiner(Naturals(), Naturals(), add)
   ```

```
>>> next(evens)
0
>>> next(evens)
2
>>> next(evens)
4

class Iter_Combiner():
    def __init__(self, iter1, iter2, combiner):




    def __next__(self):




    def __iter__(self):
```

2. What is the result of executing this sequence of commands?

```
>>> naturals = Naturals()
>>> doubled_naturals = Iter_Combiner(naturals, naturals, add)
>>> next(doubled_naturals)



>>> next(doubled_naturals)
```

3. Create an iterator that generates the sequence of Fibonacci numbers.

```
class Fibonacci_Numbers():
    def __init__(self):
```

```python
    def __next__(self):




    def __iter__(self):
```

3   Generators

A *generator* is a special kind of Python iterator that uses a `yield` statement instead of a `return` statement to report values.

Here is an iterator for the natural numbers written using the generator construct:

```python
def generate_naturals():
    current = 0
    while True:
        yield current
        current += 1
```

Calling `generate_naturals()` will return a generator object:

```
>>> gen = generate_naturals()
>>> gen
<generator object gen at ...>
```

To use the generator object, you then call `next` on it:

```
>>> next(gen)
0
>>> next(gen)
1
>>> next(gen)
2
```

Think of a generator object as containing an implicit `__next__` method. This means, **by definition**, a generator object is an iterator.

3.1 yield

The `yield` statement is similar to a `return` statement. However, while a `return` statement causes the current environment to be destroyed after a function exits, a yield statement causes the environment to be saved until the next time `__next__` is called, which allows the generator to automatically keep track of the iteration state.

Once `__next__` is called again, execution picks up from where the previously executed `yield` statement left off, and continues until the next `yield` statement (or the end of the function) is encountered.

Including a `yield` statement in a function automatically signals to Python that this function will create a generator. When we call the function, it will **return a generator object**, instead of executing the code inside the body. When the returned generator's `__next__` method is called, the code in the body is executed for the first time, and stops executing upon reaching the first `yield` statement.

A Python function can either use `return` statements or `yield` statements in the body to output values. **Having both will raise an error.**

3.2 Implementation

Because generators are technically iterators, you can implement `__iter__` methods using only generators. For example,

```python
class Naturals():
    def __init__(self):
        self.current = 0
    def __iter__(self):
        while True:
            yield self.current
            self.current += 1
```

The usage of a `Naturals` object is exactly the same as before:

```python
>>> nats = Naturals()
>>> nats_iter = iter(nats)
>>> next(nats_iter)
0
>>> next(nats_iter)
1
>>> next(nats_iter)
2
```

There are a couple of things to note:

- **No** `__next__` **method in** `Naturals`: Remember, `__iter__` just has to return an object that has implemented a `__next__` method. Since generators have their own `__next__` method, the new `Naturals` implementation is perfectly valid.

- `nats` **is a** `Naturals` **object –** `nats_iter` **is a generator**: do not treat `nats` as the iterator!

Since generators are iterators, you can also use generators in `for` loops.

3.3 Questions

1. Write a generator function that returns lists of all subsets of the positive integers from 1 to n. Each call to this generator's `__next__` method will return a list of subsets of the set `[1, 2, ..., n]`, where `n` is the number of times `__next__` was previously called.

```
>>> subsets = generate_subsets()
>>> next(subsets)
[[]]
>>> next(subsets)
[[], [1]]
>>> next(subsets)
[[], [1], [2], [1, 2]]

def generate_subsets():
```

2. Define a generator that yields the sequence of perfect squares.

```
def perfect_squares():
```

3. Remember the hailstone sequence from homework 1? Implement it using a generator! To generate a hailstone sequence:

- Pick a positive number n

- If n is even, divide it by 2

- If n is odd, multiply it by 3 and add 1

- Continue this process until n is 1

```python
def generate_hailstone(n=10):
```

4   Streams

A *stream* is our third example of a lazy sequence. A stream is a lazily evaluated RList. In other words, the stream's elements (except for the first element) are only evaluated when the values are needed.

Take a look at the following code:

```python
class Stream(object):
    class empty(object):
        def __repr__(self):
            return 'Stream.empty'

    empty = empty()

    def __init__(self, first, compute_rest, empty= False):
        self.first = first
        self._compute_rest = compute_rest
        self.empty = empty
        self._rest = None
        self._computed = False

    @property
    def rest(self):
        assert not self.empty, 'Empty streams have no rest.'
        if not self._computed:
```

```
            self._rest = self._compute_rest()
            self._computed = True
        return self._rest

    def __repr__(self):
        return 'Stream({0}, <...>)'.format(repr(self.first))
```

We represent Streams using Python objects, similar to the way we defined RLists. We nest streams inside one another, and compute one element of the sequence at a time.

Note that instead of specifying all of the elements in __init__, we provide a function, compute_rest, that encapsulates the algorithm used to calculate the remaining elements of the stream. Remember that the code in the function body is not evaluated until it is called, which lets us implement the desired evaluation behavior.

This implementation of streams also uses *memoization*. The first time a program asks a Stream for its rest field, the Stream code computes the required value using compute_rest, saves the resulting value, and then returns it. After that, every time the rest field is referenced, the stored value is simply returned and it is not computed again.

Here is an example:

```
def make_integer_stream(first=1):
    def compute_rest():
        return make_integer_stream(first+1)
    return Stream(first, compute_rest)
```

Notice what is happening here. We start out with a stream whose first element is 1, and whose compute_rest function creates another stream. So when we do compute the rest, we get another stream whose first element is one greater than the previous element, and whose compute_rest creates another stream. Hence, we effectively get an infinite stream of integers, computed one at a time. This is almost like an infinite recursion, but one which can be viewed one step at a time, and so does not crash.

4.1 Questions

1. Write a procedure make_fib_stream() that creates an infinite stream of Fibonacci Numbers. Make the first two elements of the stream 0 and 1.

   Hint: Consider using a helper procedure that can take two arguments, then think about how to start calling that procedure.

   ```
   def make_fib_stream():
   ```

2. Write a procedure `sub_streams` that takes in two streams `s1`, `s2`, and returns a new stream that is the result of subtracting elements from `s1` by elements from `s2`. For instance, if `s1` was `(1, 2, 3, ...)` and `s2` was `(2, 4, 6, ...)`, then the output would be the stream `(-1, -2, -3, ...)`. You can assume that both Streams are infinite.

```
def sub_streams(s1, s2):
```

3. Define a procedure that inputs an infinite Stream, `s`, and a target value and returns `True` if the stream converges to the target within a certain number of values. For this example we will say the stream converges if the difference between two consecutive values and the difference between the value and the target drop below `max_diff` for 10 consecutive values. (*Hint*: create the stream of differences between consecutive elements using `sub_streams`)

```
def converges_to(s, target, max_diff=0.00001, num_values=100):
```

4.2 Higher Order Functions on Streams

Naturally, as the theme has always been in this class, we can abstract our stream procedures to be higher order. Take a look at filter_stream:

```python
def filter_stream(filter_func, stream):
    def make_filtered_rest():
        return filter_stream(filter_func, stream.rest)
    if Stream.empty:
        return stream
    elif filter_func(stream.first):
        return Stream(stream.first, make_filtered_rest)
    else:
        return filter_stream(filter_funct, stream.rest)
```

You can see how this function might be useful. Notice how the Stream we create has as its compute_rest function a procedure that "promises" to filter out the rest of the Stream when asked. So at any one point, the entire stream has not been filtered. Instead, only the part of the stream that has been referenced has been filtered, but the rest will be filtered when asked. We can model other higher order Stream procedures after this one, and we can combine our higher order Stream procedures to do incredible things!

4.3 Questions

1. In a similar model to filter_stream, let's recreate the procedure map_stream from lecture, that given a stream stream and a one-argument function func, returns a new stream that is the result of applying func on every element in stream.

   ```python
   def stream_map(func, stream):
   ```

2. What does the following Stream output? Try writing out the first few values of the
   stream to see the pattern.

```
def my_stream():
    def compute_rest():
        return add_streams(map_stream(double,
                                      my_stream()),
                           my_stream())
    return Stream(1, compute_rest)
```