## CS 61b: Final Review

## **Data Structures**

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## **DISCLAIMER**

We have NOT seen the exam. We do NOT know the format of the exam

What we are presenting is what we "think is important" for the exam

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Final Review

## Review Topics

- Inheritance, Method Calls
- Asymptotic Analysis
- Data Structures
- Binary Search Trees
- B-Trees
- Heaps
- Hash Tables
- AVL Trees
- Graphs
  - DFS, BFS
  - Topological Sort
  - Strongly Connected Components

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Dijkstra

Kruskal

Sorting Skip Lists

Scheduling

Minimax

B+ Trees Threaded Trees

Threading, Synchronization

## Inheritance/Method Calls

• Given the class definitions on the next slide, which lines in class foobarbaz are illegal?

## package foo; Inheritance import bar.bar; package foo; public class foobarbaz { static void main(String[] args) { public class foo { foo f = new foo();static void f1() {...} bar r = new bar();protected boolean f2(int x) {...} baz z; private String f3(String s) {...} r.f3(3); f.f2(3); package foo; z = (baz) f;public class baz extends foo { f = new baz();private String f3(String s) {...} f.f2(3); z = (baz) f;z.f1(); package bar; import foo.foo; r.f1(); public class bar extends foo { ((foo) r).f1(); protected boolean f3(int x) {...} Amir Kamil and Jack Sampson

## Inheritance/Method Calls

Access table:

	world	package	child	definer
public	Х	Х	Х	Х
private				Х
protected		Х	Х	Х
<default></default>		Х		Х

- Static methods called according to static type
- Child type can be assigned to parent variable without a cast, but the reverse requires one, and the dynamic types must match

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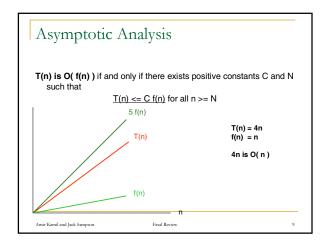
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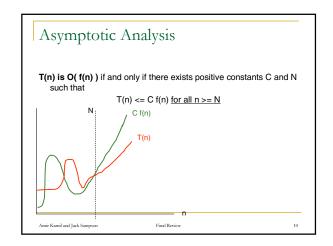
```
package foo;
  Inheritance
                                      import bar.bar;
                                      public class foobarbaz {
package foo;
                                        static void main(String[] args) {
public class foo {
                                           foo f = new foo();
   static void f1() {...}
                                           bar r = new bar();
   protected boolean f2(int x) {...}
                                           baz z;
   private String f3(String s) {...}
                                                               // ILLEGAL
                                           r.f3(3);
                                           f.f2(3);
package foo;
                                                               // ILLEGAL
                                           z = (baz) f;
public class baz extends foo {
                                           f = new baz();
  private String f3(String s) {...}
                                           f.f2(3):
                                           z = (baz) f;
package bar;
                                           z.f1();
                                                              // ILLEGAL
import foo.foo;
                                           r.f1();
                                           ((foo) r).f1();
public class bar extends foo {
  protected boolean f3(int x) { ...
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```

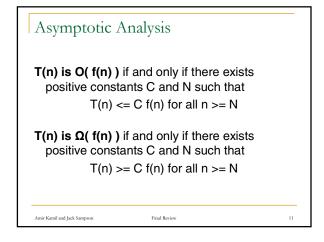
```
Asymptotic Analysis

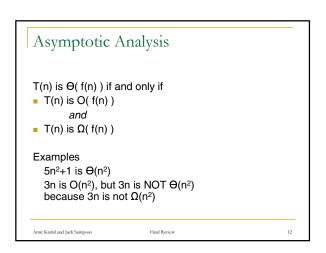
O – Upper bound/Worst case
Ω – Lower bound
Θ – both
ο – strictly Upper bound

More detail...
```







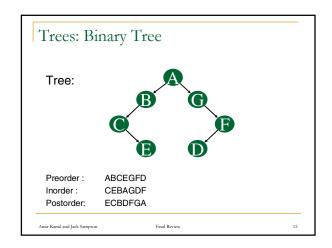


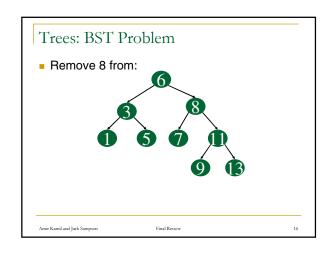
## Asymptotic Analysis Problem Find the running time of the following code: int foo(int x) { int ans = 1; for (int i = 0; i < x; i++) { for (int j = 0; j < i; j++) { ans \*= (i + j); } } return ans; }

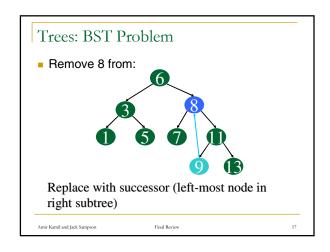
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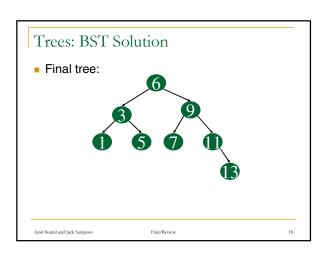
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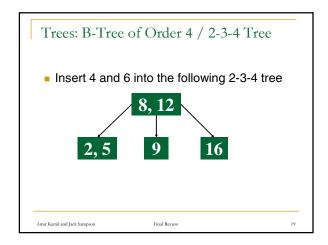
## Asymptotic Analysis Solution The nested loops give away the answer: the outer loop executes x times, the inner loop an average of x/2 times, for a running time of $O(x^2)$ . int foo(int x) { int ans = 1; for (int i = 0; i < x; i++) { for (int j = 0; j < i; j++) { ans \*= (i + j); } } return ans; }

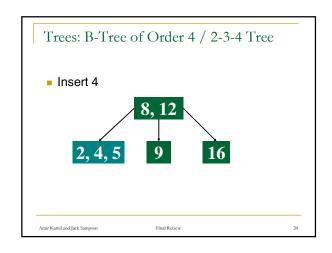


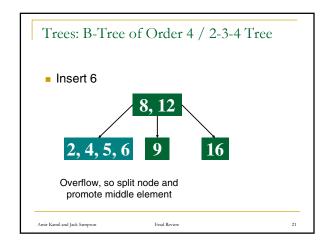


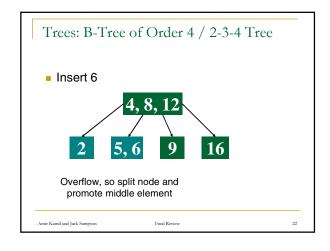


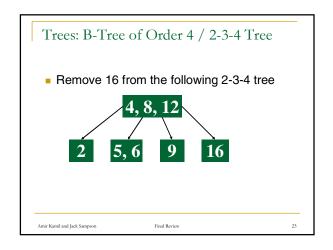


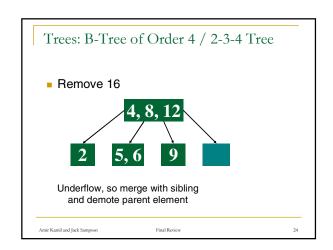


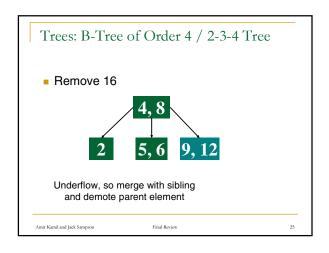


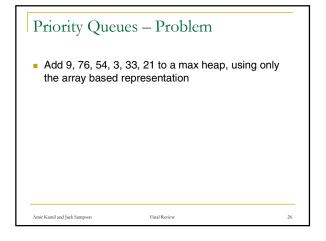


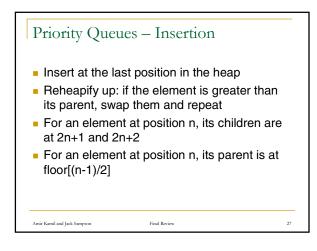


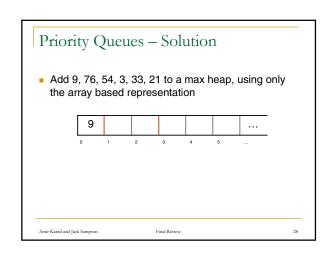


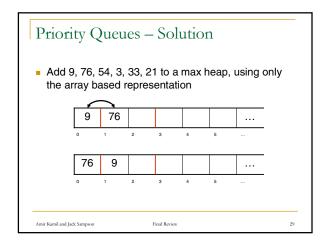


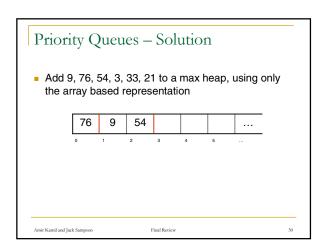


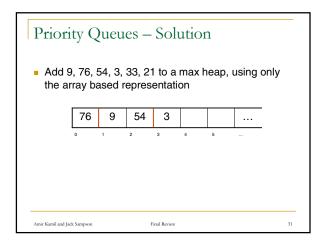


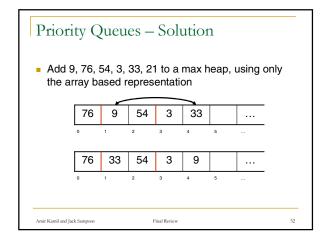


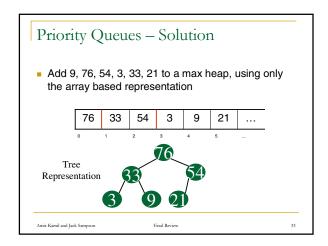


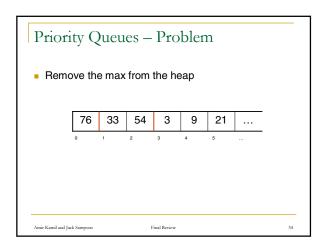


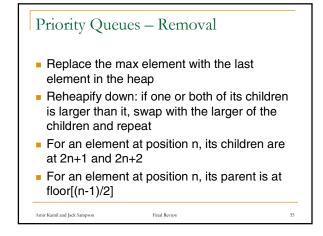


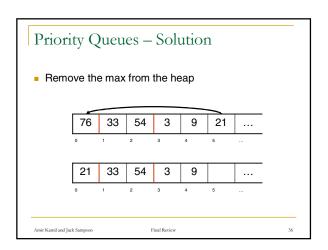


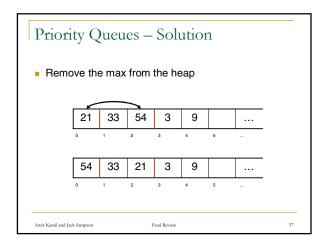


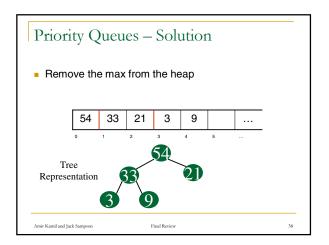












## Hash Table Problem

 Draw the structure of a size 7 hash table after insertion of keys with the following hash codes: 0, 95, 21, 6, 64, 74, 3, 54, 34, 75, 10.

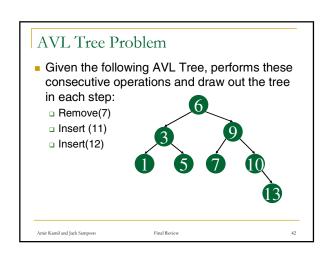
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## Hash Tables

- High-level idea 2 components
  - 1. Big array called hash table of size M
  - 2. Function *h* which maps keys to integer values
- For (key, item), use h(key) % M to find location of item in table
- Linked list in each entry that stores all items that map to that location (chaining)

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## Hash Table Solution • Draw the structure of a size 7 hash table after insertion of keys with the following hash codes: 0, 95, 21, 6, 64, 74, 3, 54, 34, 75, 10. Amir Kamil and Jack Sampson Final Review 41



## AVL Trees

- AVL Trees are just Binary Search Trees that can rotate their nodes to try to maintain balance.
  - □ Two kinds of rotations single and double
  - Can decide which to do based on structure of tree

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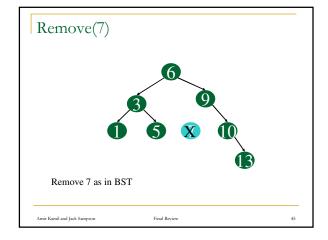
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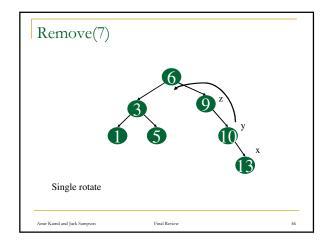
## Insertions/Removals

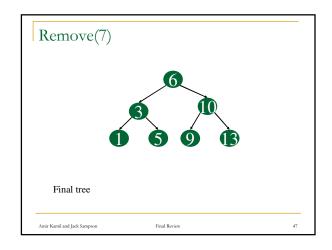
- You have 3 nodes of importance, which we will call x, y, and z (z is the parent of y which is the parent of x)
  - If x is the right child of y, and y is the right child of z, you do a single rotation (same goes for left child of left child)
  - If x is the right child of y, and y is the left child of z, you do a double rotation (same goes for left child of right child)

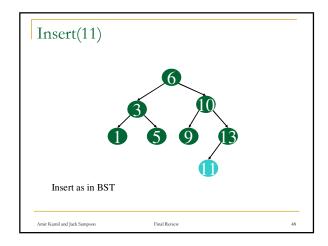
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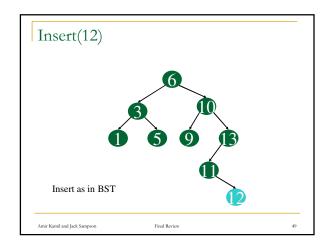
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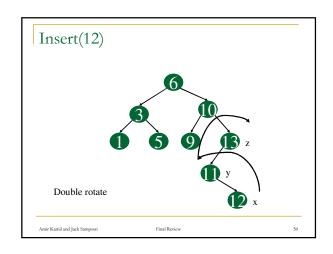


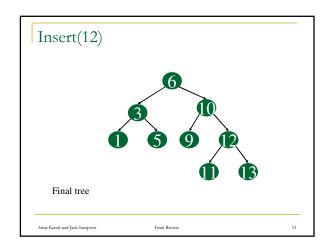


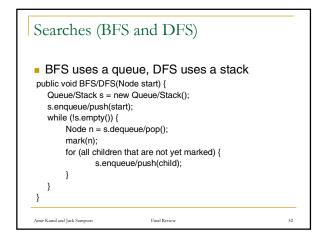


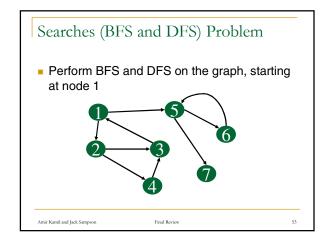


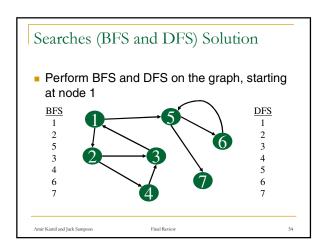


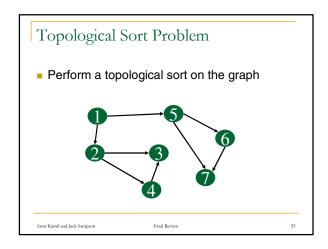


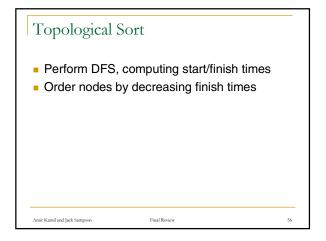


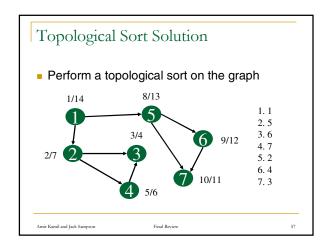


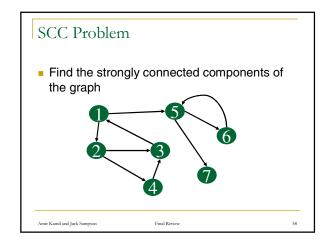


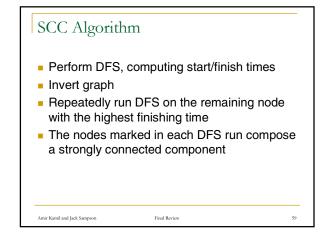


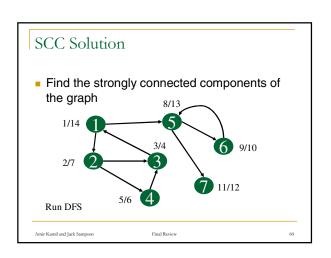


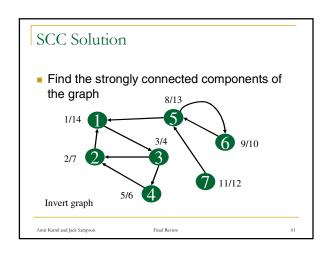


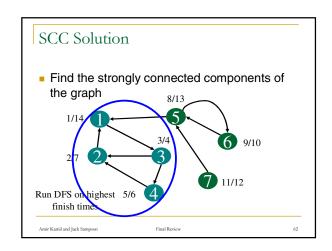


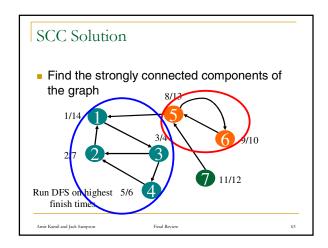


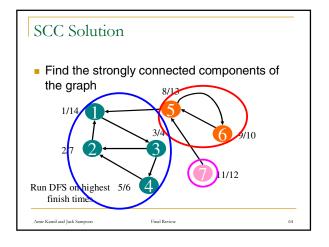


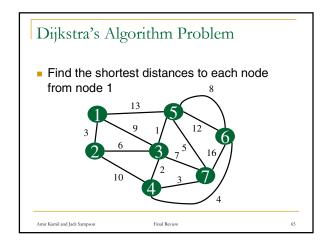


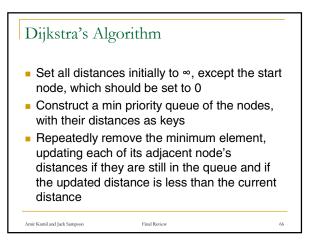


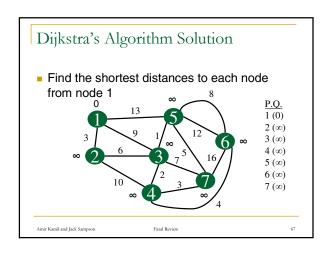


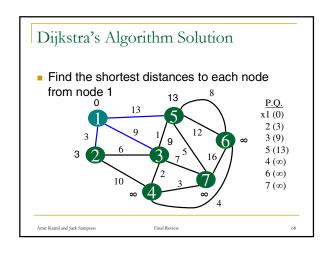


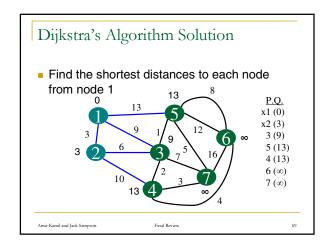


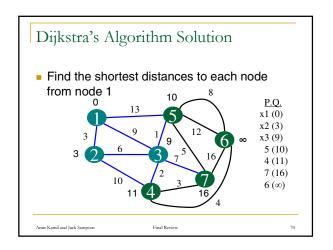


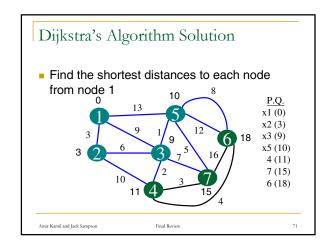


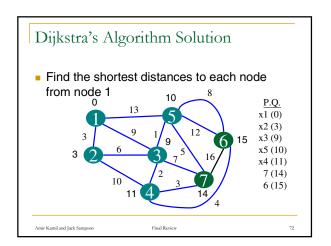


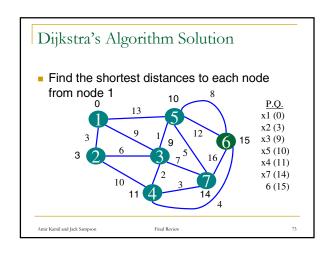


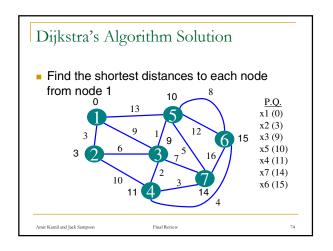


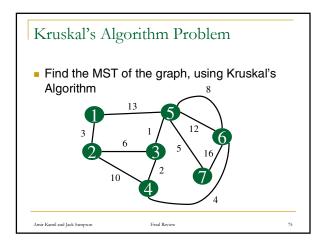


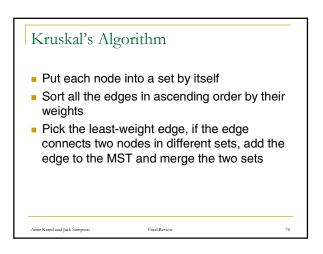


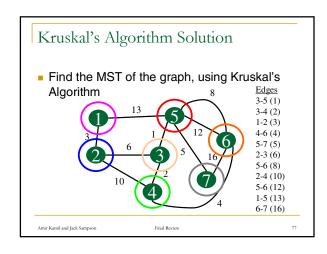


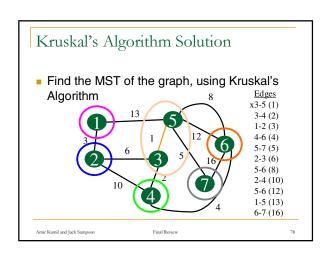


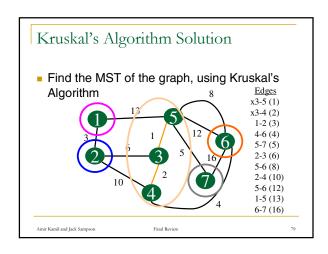


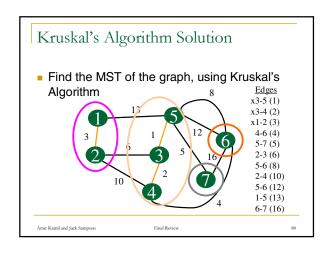


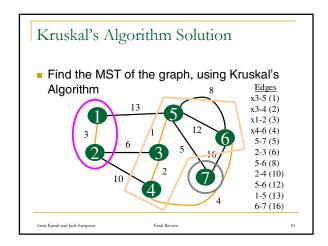


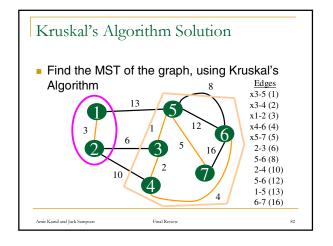


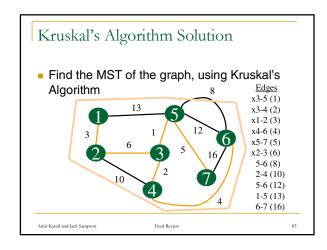


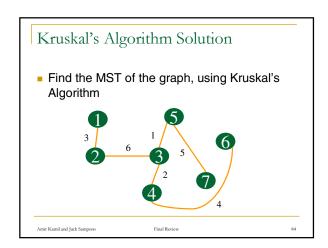


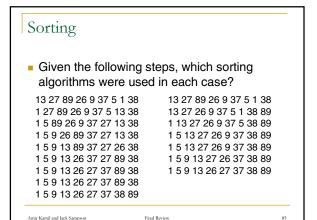


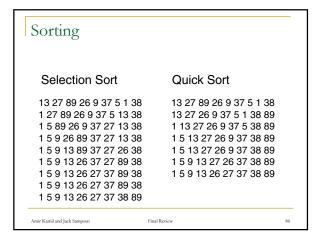


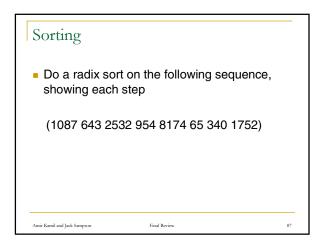




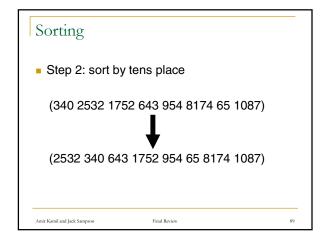






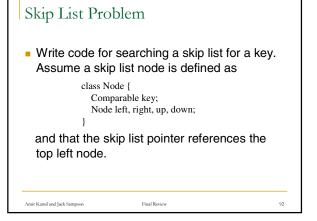




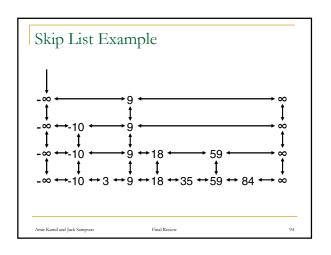








## Skip Lists D linked lists Bottom level contains all keys, and each subsequent level contains probabilistically half the keys of the previous level Each level starts at -∞ and ends at +∞ The keys in each level are in ascending order



## Skip List Searching

- Start at top left node
- If the current key is equal to the search key, return the node
- If the next key is greater than the search key, go down and repeat search
- Otherwise go right and repeat search

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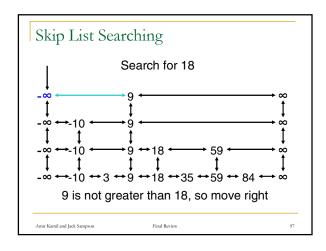
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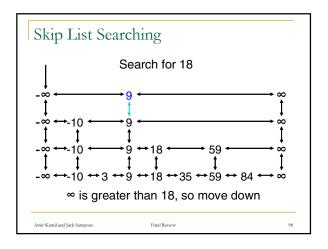
## Skip List Solution

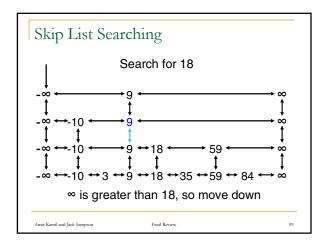
Write code for searching a skip list for a key

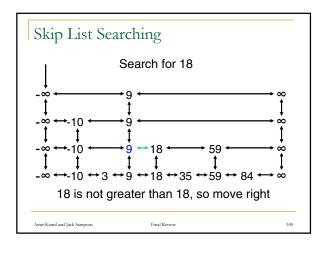
```
Node search(Node n, Comparable key) {
    if (n.key.equals(key)) {
        return n;
    } else if (n.next.key.compareTo(key) > 0) {
        return search(n.down, key);
    } else {
        return search(n.next, key);
    }
}

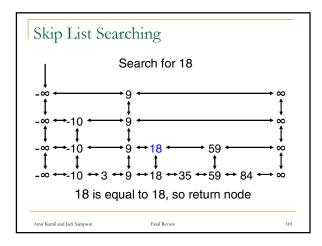
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```













## Scheduling

- Throughput Average number of tasks completed per unit time
- CPU Utilization Average usage of the processor
- Wait time time spent waiting for processor
- Turnaround time time from task assignment to task completion
- Response time time between assignment of task and first work on task
- Large values => GOOD:
  - throughput
  - cpu utilization
- Large values => BAD (maybe):
  - wait time
- turnaround time
- response time
- I/O ?

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Final Review

## The Min-Max Algorithm

An algorithm for making the best possible move in a ZERO-SUM-GAME (not applicable to other types of games)

```
MinMax( State, maxtype)
  if gameover(State) return [null move, score(State)]
  if (maxtype)
    return pair with max score from
     for each valid move from State MinMax(NewState, !
  maxtype)
  else
    return pair with min score from
      for each valid move from State MinMax(NewState, !
```

## Justification:

 In a zero-sum-game, the best move for an opponent is to minimize your score, just as your best move is to maximize your score. This will therefore return the best possible move under the assumption that one's opponent plays perfectly.

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## The Min-Max Algorithm

■ The following is an implementation of Min-Max in Common Lisp:

- "The minima decision procedure returns the opinima move in the game "Limb minima decision procedure returns the opinima move in the game issuing enhancing sensention of the entire game rese. Implementation uses the fact that the evaluation and utility functions return a fast of issuing the point of view of each player, with the "current" player first. Hence, suther than using first, we always use firsts of ingit-relation. This works for any number of players. "The notation" ser's means an (action, satelp jair.

#'(lambda (a+s) (first (right-rotate (minimax-value (cdr a+s) game)))) (game-successors state game))))

(defun minimax-value (state game) (if (game-over? game state)

(terminal-values state)

(right-rotate

(Ingini-vicate
(the-biggest
#'(lambda (values) (first (right-rotate values)))
(mapcar #'(lambda (a+s) (minimax-value (cdr a+s) game))

(game-successors state game))))))

## Min-Max with cutoff

(defun minimax-cutoff-decision (state game eval-fn limit)
"Return the best action, according to backed-up evaluation down to LIMIT.
After we search LIMIT levels seep, we use EVAL-Fn to provide an estimate of the true value of a state; thus the action may not actually be best." (car (the-biggest

#'(lambda (a+s)

(first (right-rotate (minimax-cutoff-value (cdr a+s) game eval-fn (- limit 1))))) (game-successors state game))))

(defun minimax-cutoff-value (state game eval-fn limit) (cond ((game-over? game state) (terminal-values state)) ((<= limit 0) (funcall eval-fn state))

#'(lambda (values) (first (right-rotate values)))

(mapcar #'(lambda (a+s) (minimax-cutoff-value (cdr a+s) game eval-fn

(game-successors state game)))))))

## Min-Max with cutoff

(defun game-successors (state game)
"Return a list of (move. state) pairs that can be reached from this state."
(mapcar #[lambda (move) (cons move (make-move game state move)))
(legal-moves game state)))

"Return the values of the state for each player."
(mapcar #'(lambda (player) (getf (game-state-scores state) player))
(game-state-players state)))

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## alpha-beta pruning

(defun alpha-beta-decision (state game eval-fn &optional (limit 4))

"Return the estimated best action, searching up to LIMIT and then applying the EVAL-FN."

(are (the-biggest # gambda (a+s))

(first dictor set to the set of the s

(first (right-rotate

(alpha-value (cdr a+s) game

(game-worst game) (game-worst game) eval-fn (- limit 1)))))

(defun alpha-value (state game alpha beta eval-fn limit) (cond ((game-over? game state) (terminal-values state))

((= 0 limit) (funcall eval-fn state))

(t (dolist (a+s (game-successors state game) (list alpha (- alpha)))

(setq alpha (max alpha (first (right-rotate

(beta-value (cdr a+s) game alpha beta

(when (>= alpha (- beta))

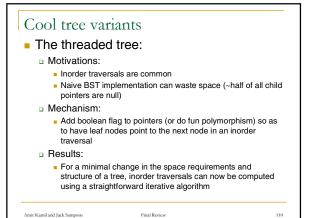
(return (list (- beta) beta))))))

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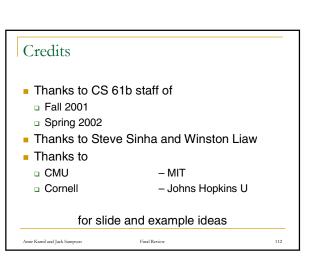
eval-fn (- limit 1))))))

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# alpha-beta pruning (defun beta-value (state game alpha beta eval-in limit) (cond ((game-over) game state) (terminal-values state)) ((=0 limit) (tuncal eval-nf state)) (t (doist (a+s (game-auccessors state game)) (set (peta (max beta (first (right-rotate (a)pha-value (cdr a+s) game alpha beta eval-in (- limit 1)))))) (when (>= beta (- alpha)) (return (list (- alpha) alpha)))))) Amir Kamal and Jack Sampson Final Review 109



# Cool tree variants continued The B+ tree: Motivations: Range queries are common size of Data >> size of Key, so treat differently Mechanism: Start with B-tree Differentiate between Leaf and index nodes. Index nodes hold keys, leaf nodes hold data. Key values for all data are in leaf nodes. Insert and delete as before, except keys are copied up on split, not moved, and keys may remain on delete for data that no longer exists Add next and previous fields to all leaf nodes, forming a doubly linked list Results: Range query now straightforward to return result for - tree now optimized for contiguous storage on physical media



GOOD LUCK!
(and may you not need it)

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