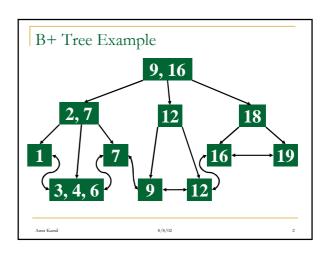
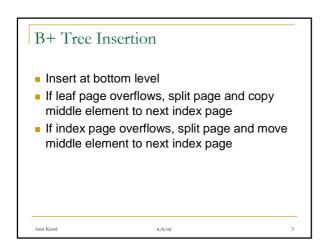
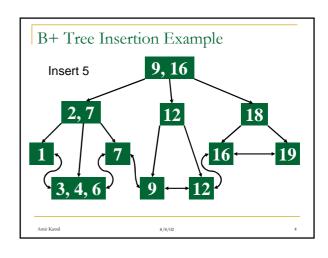
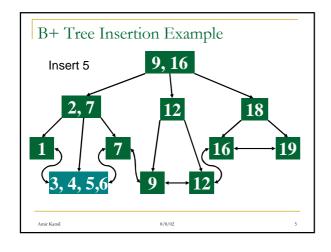
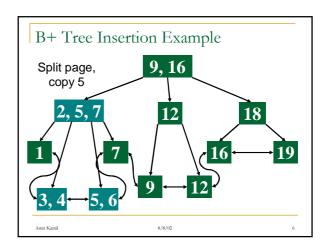
B+ Trees Similar to B trees, with a few slight differences All data is stored at the leaf nodes (*leaf pages*); all other nodes (*index pages*) only store keys Leaf pages are linked to each other Keys may be duplicated; every key to the right of a particular key is >= to that key

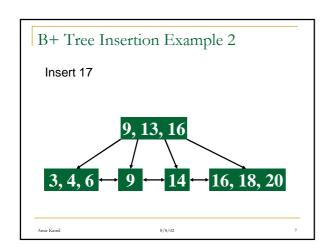


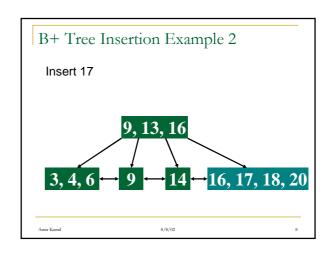


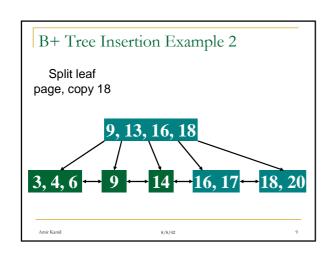


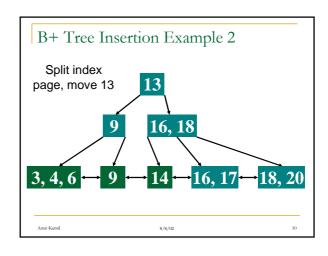


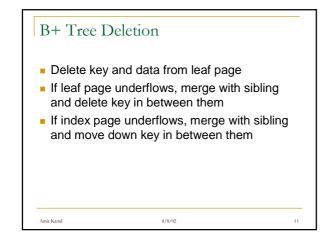


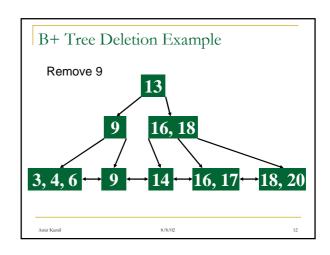


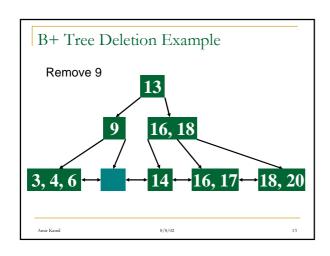


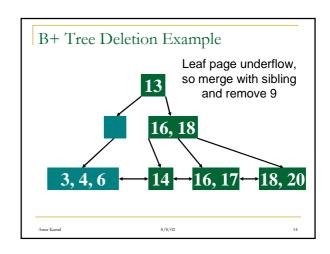


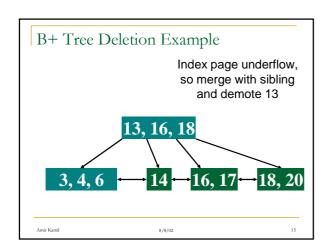




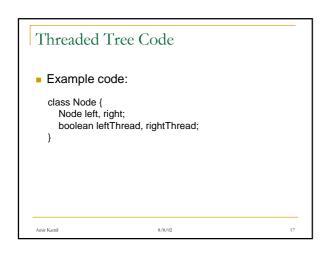


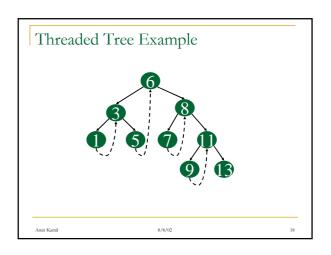




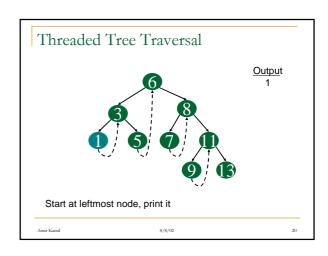


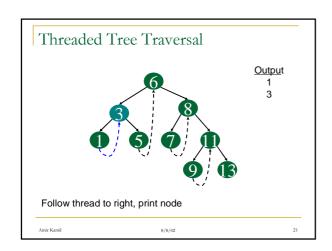
Threaded Trees Binary trees have a lot of wasted space: the leaf nodes each have 2 null pointers We can use these pointers to help us in inorder traversals We have the pointers reference the next node in an inorder traversal; called *threads*We need to know if a pointer is an actual link or a thread, so we keep a boolean for each pointer

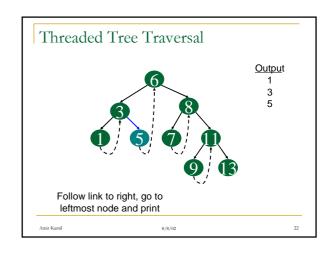


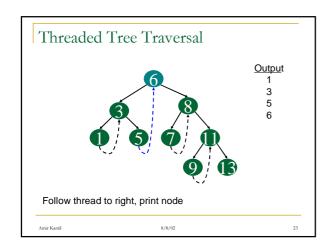


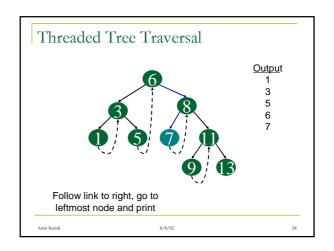
Threaded Tree Traversal We start at the leftmost node in the tree, print it, and follow its right thread If we follow a thread to the right, we output the node and continue to its right If we follow a link to the right, we go to the leftmost node, print it, and continue

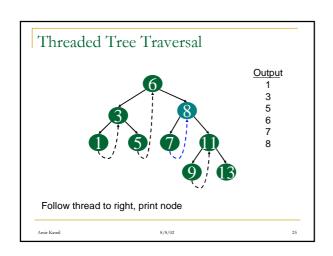


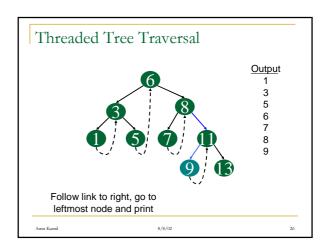


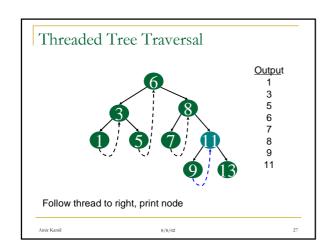


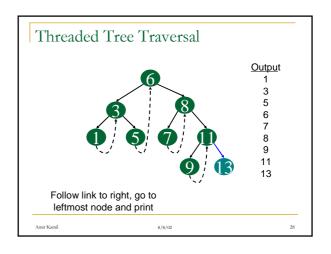












Threaded Tree Modification We're still wasting pointers, since half of our leafs' pointers are still null We can add threads to the previous node in an inorder traversal as well, which we can use to traverse the tree backwards or even to do postorder traversals

