



# CS61A Lecture 39

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UC Berkeley

April 22, 2013

# Announcements



- HW12 due Wednesday
- Scheme project, contest due next Monday

# Databases



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SQL is an example of a declarative programming language.

It separates *what* to compute from *how* it is computed

The language interpreter is free to compute the result in any way it deems appropriate

[http://www.headfirstlabs.com/sql\\_hands\\_on/](http://www.headfirstlabs.com/sql_hands_on/)

# Declarative Programming



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They typically trade off data scale for problem complexity

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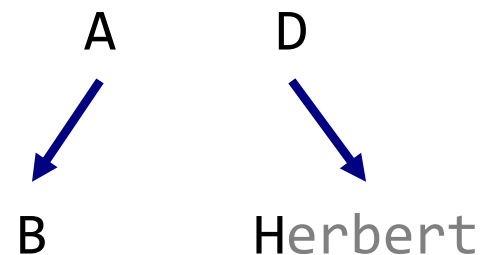
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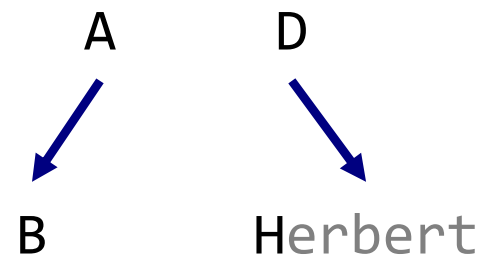
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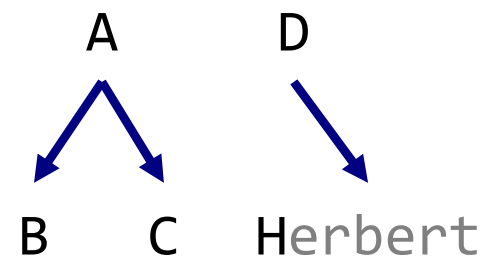
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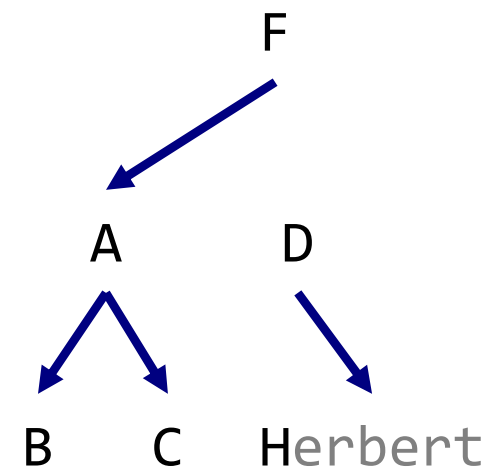
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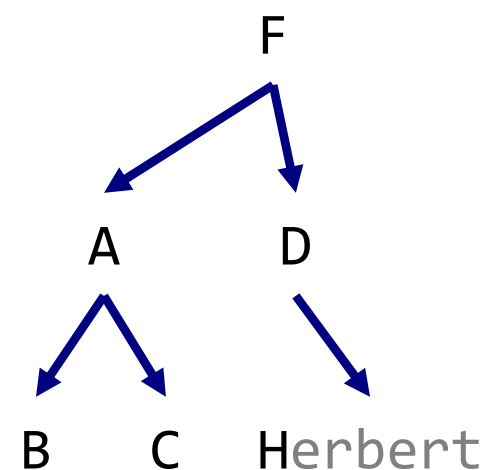
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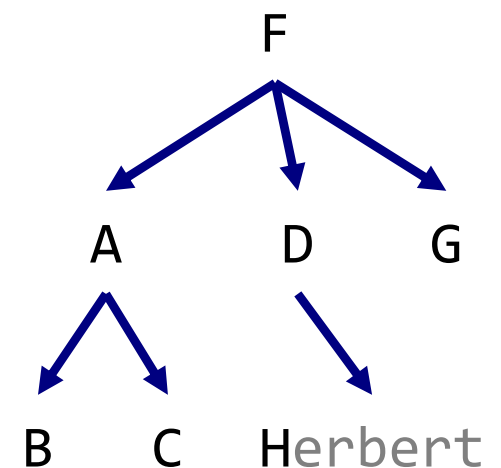
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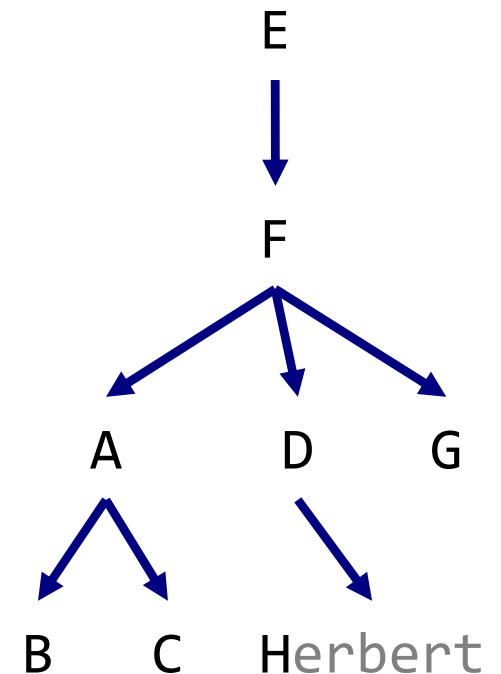
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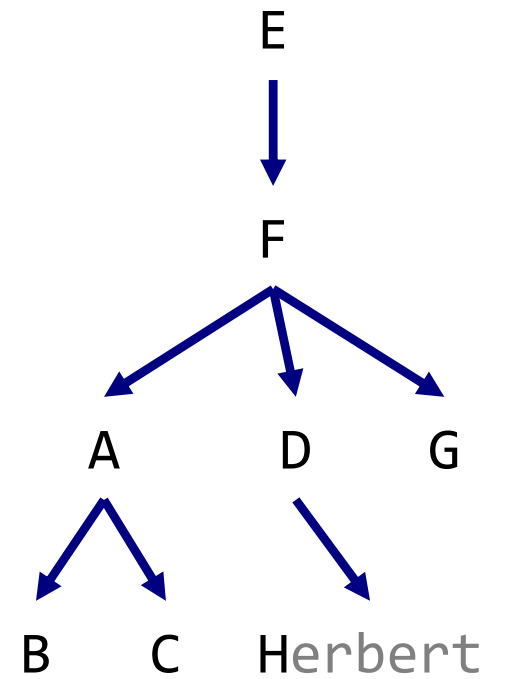
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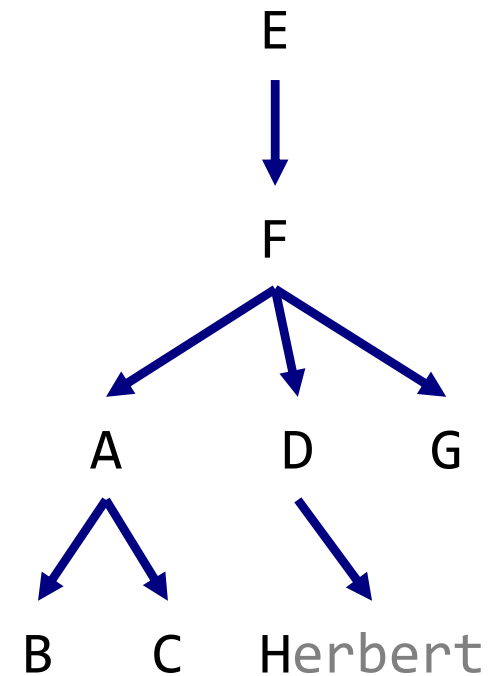




# Queries



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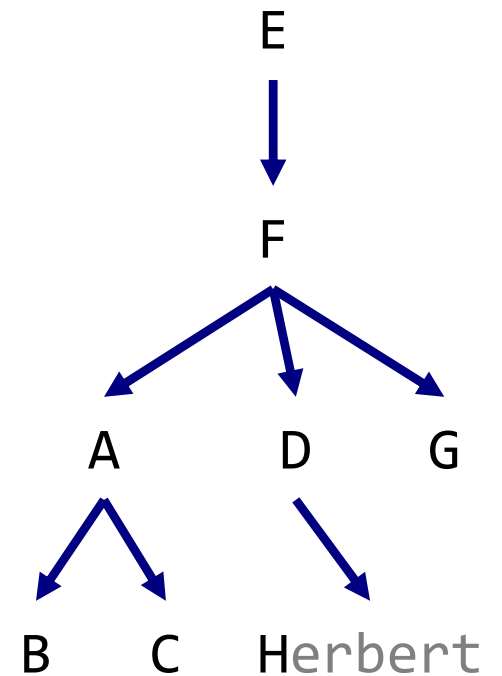


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Queries may contain variables: symbols starting with ?



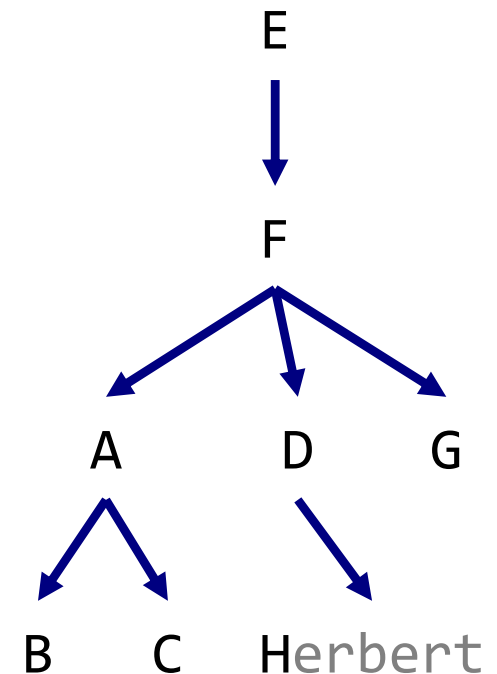
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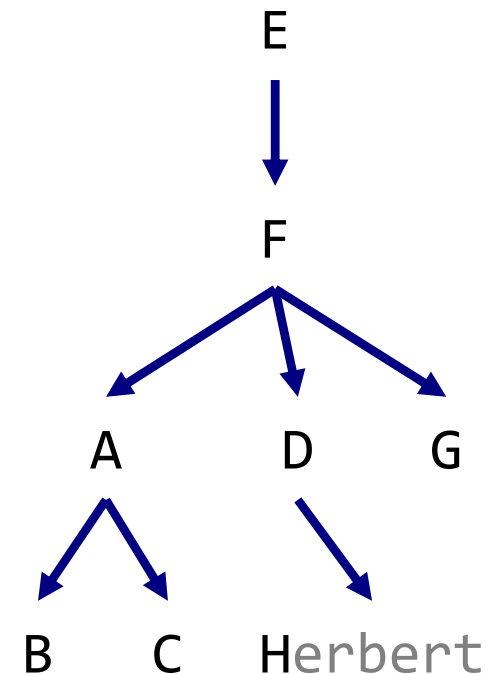


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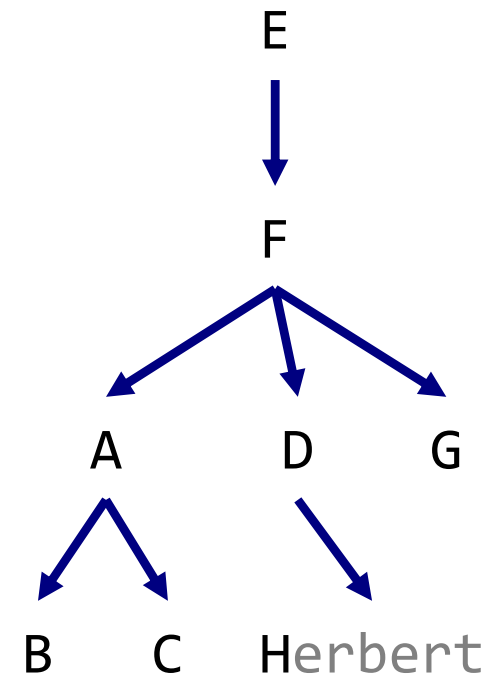


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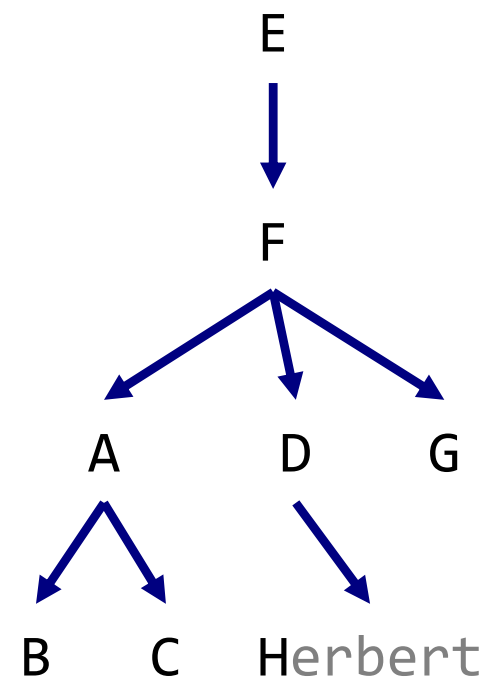


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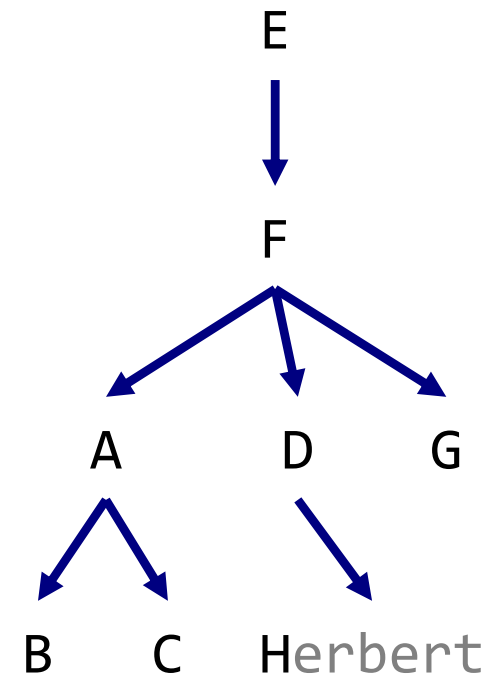


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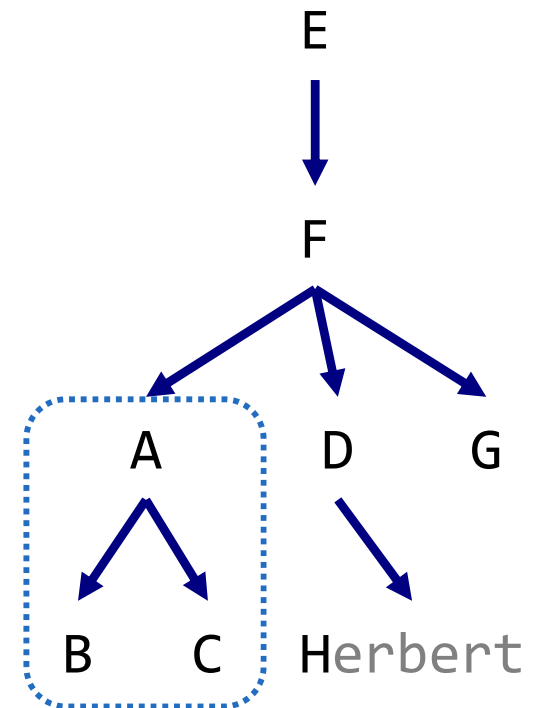
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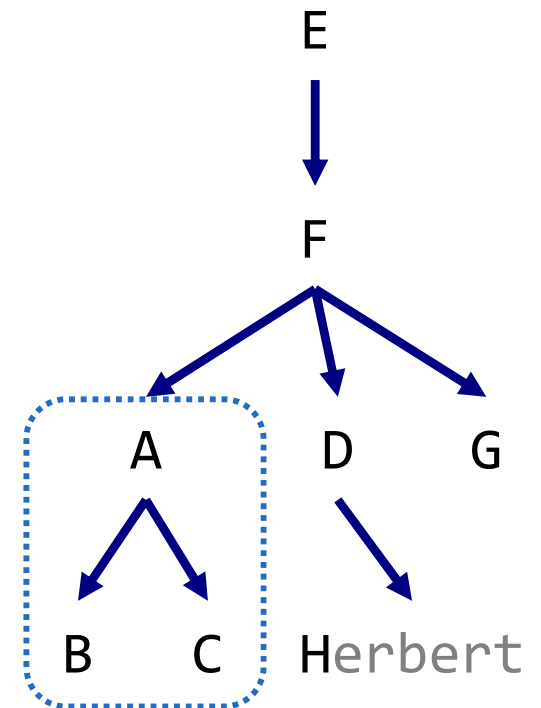
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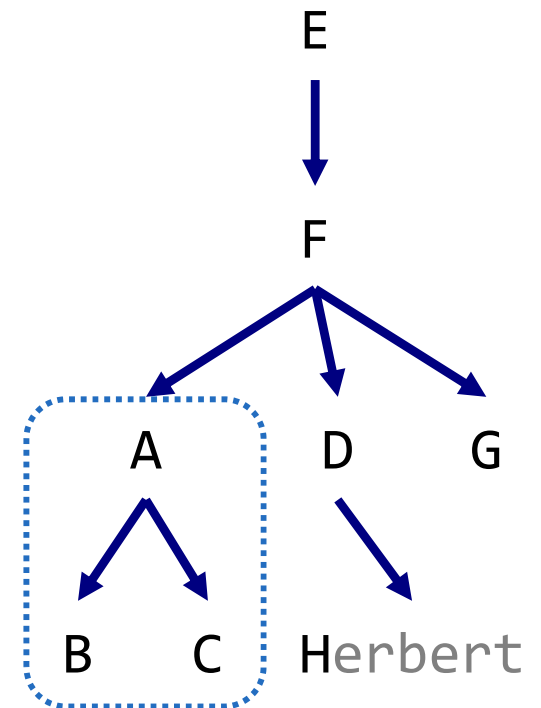


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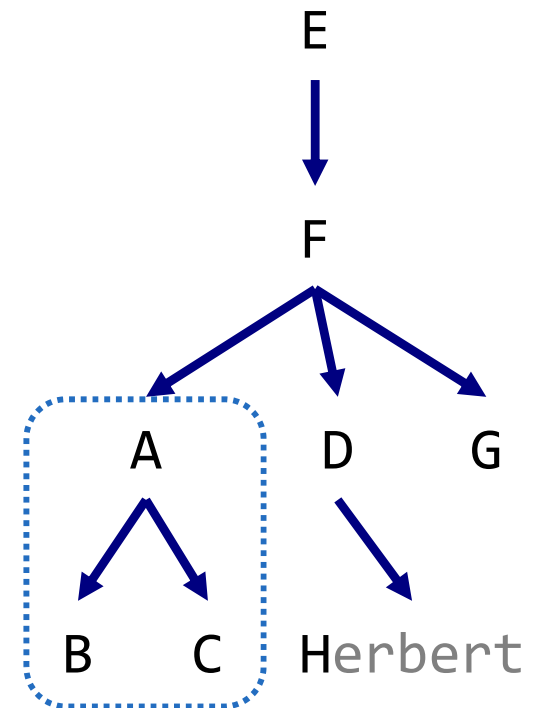


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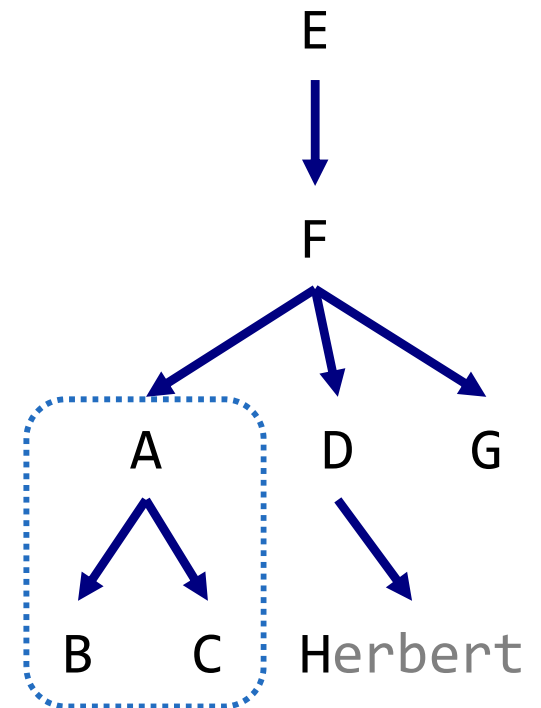
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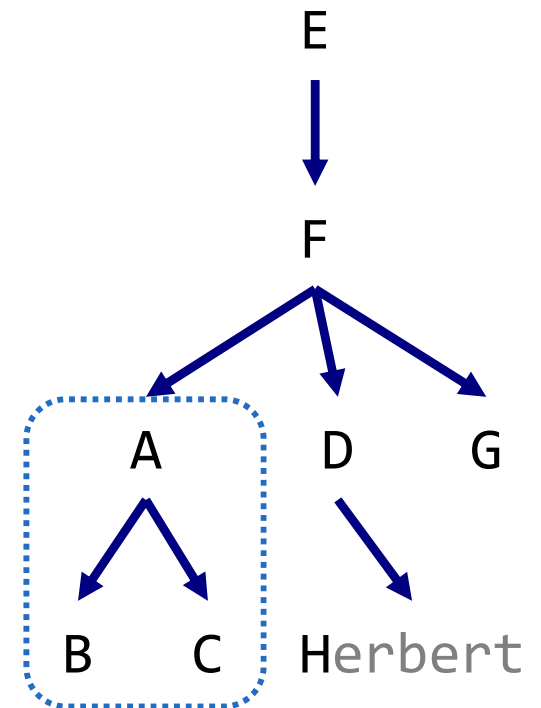
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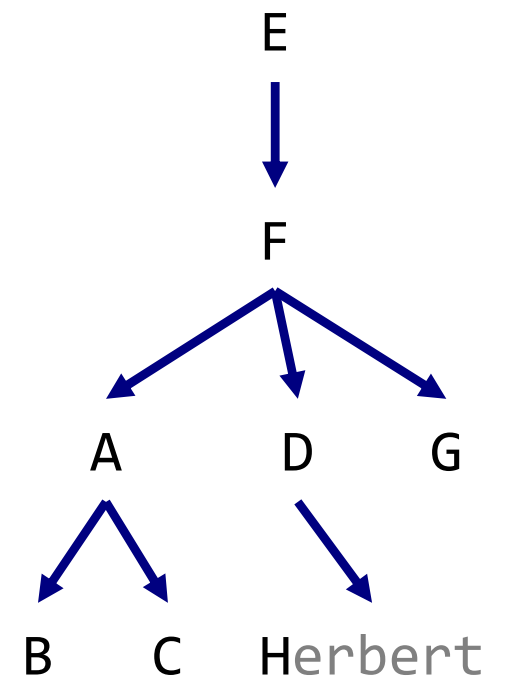
logic> (query (parent ?who barack)
              (parent ?who clinton))
```

Success!

who: abraham



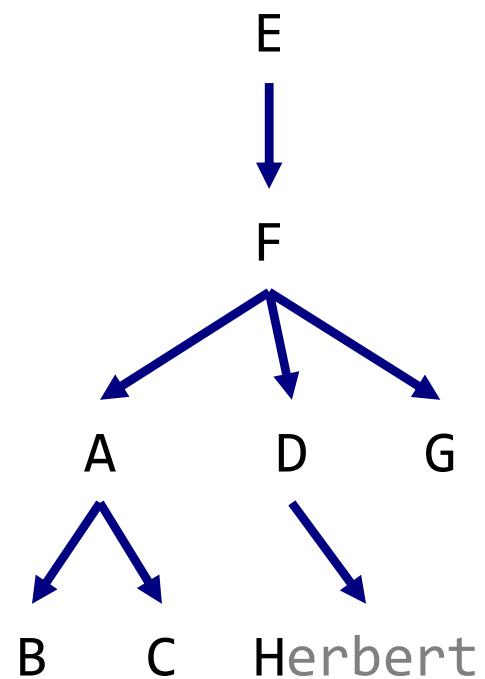
# Compound Facts



# Compound Facts



A fact can include multiple relations and variables as well

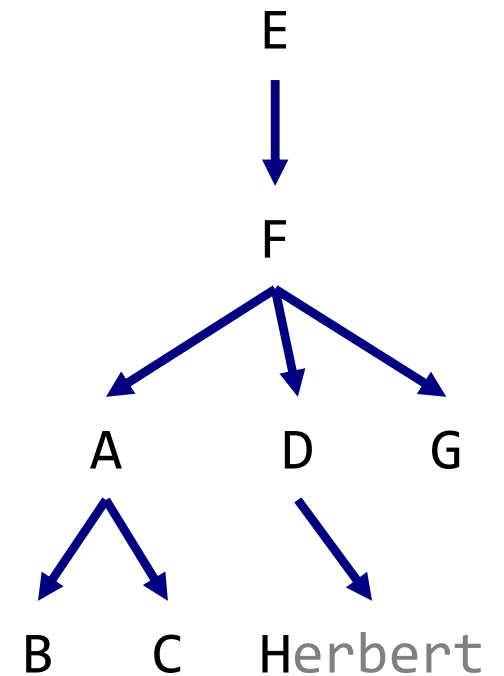


# Compound Facts



A fact can include multiple relations and variables as well

(fact <conclusion> <hypothesis<sub>0</sub>> <hypothesis<sub>1</sub>> ... <hypothesis<sub>N</sub>>)





# Compound Facts

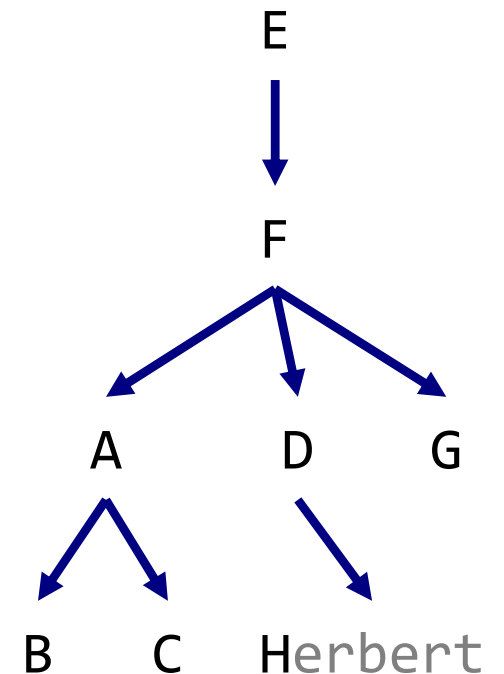


A fact can include multiple relations and variables as well

(fact <conclusion> <hypothesis<sub>0</sub>> <hypothesis<sub>1</sub>> ... <hypothesis<sub>N</sub>>)

Means <conclusion> is true if all <hypothesis<sub>K</sub>> are true

hesis<sub>N</sub>>)



# Compound Facts

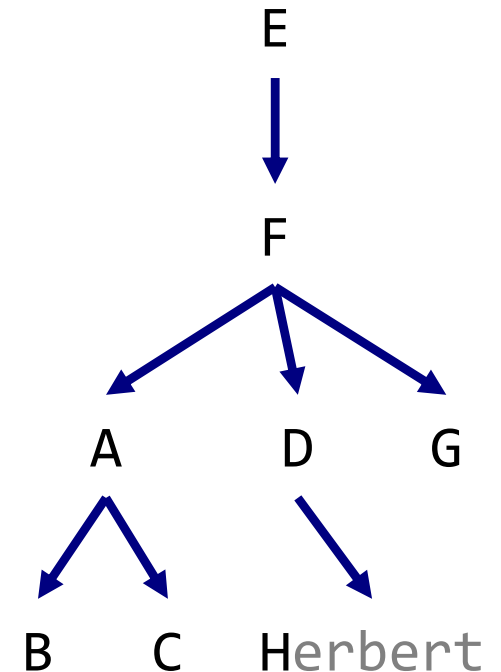


A fact can include multiple relations and variables as well

```
(fact <conclusion> <hypothesis0> <hypothesis1> ... <hypothesisN>)
```

Means **<conclusion>** is true if all **<hypothesis<sub>K</sub>>** are true

```
(fact (child ?c ?p) (parent ?p ?c))
```



# Compound Facts



A fact can include multiple relations and variables as well

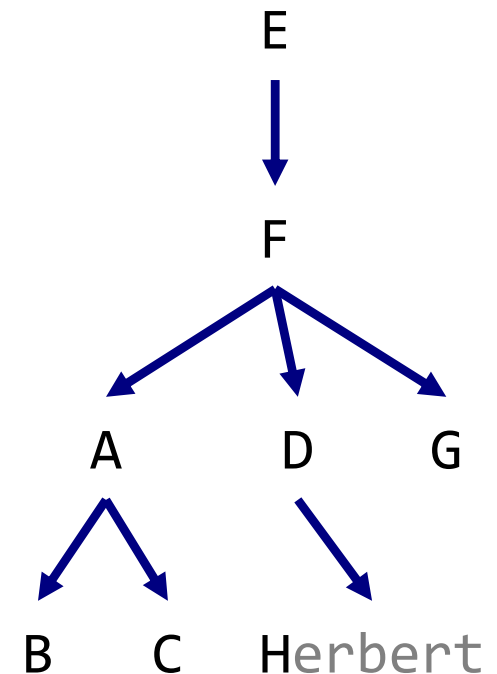
```
(fact <conclusion> <hypothesis0> <hypothesis1> ... <hypothesisN>)
```

Means **<conclusion>** is true if all **<hypothesis<sub>K</sub>>** are true

```
logic> (fact (child ?c ?p) (parent ?p ?c))
```

```
logic> (query (child herbert delano))
```

Success!



# Compound Facts



A fact can include multiple relations and variables as well

```
(fact <conclusion> <hypothesis0> <hypothesis1> ... <hypothesisN>)
```

Means **<conclusion>** is true if all **<hypothesis<sub>K</sub>>** are true

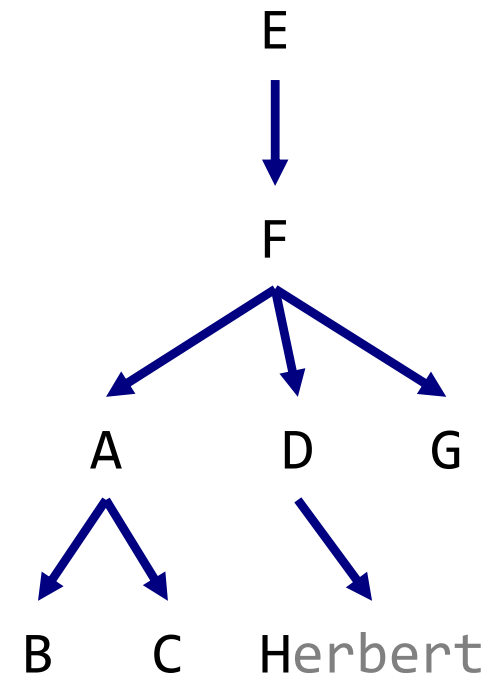
```
logic> (fact (child ?c ?p) (parent ?p ?c))
```

```
logic> (query (child herbert delano))
```

Success!

```
logic> (query (child eisenhower clinton))
```

Failure.



# Compound Facts



A fact can include multiple relations and variables as well

```
(fact <conclusion> <hypothesis0> <hypothesis1> ... <hypothesisN>)
```

Means **<conclusion>** is true if all **<hypothesis<sub>K</sub>>** are true

```
logic> (fact (child ?c ?p) (parent ?p ?c))
```

```
logic> (query (child herbert delano))
```

Success!

```
logic> (query (child eisenhower clinton))
```

Failure.

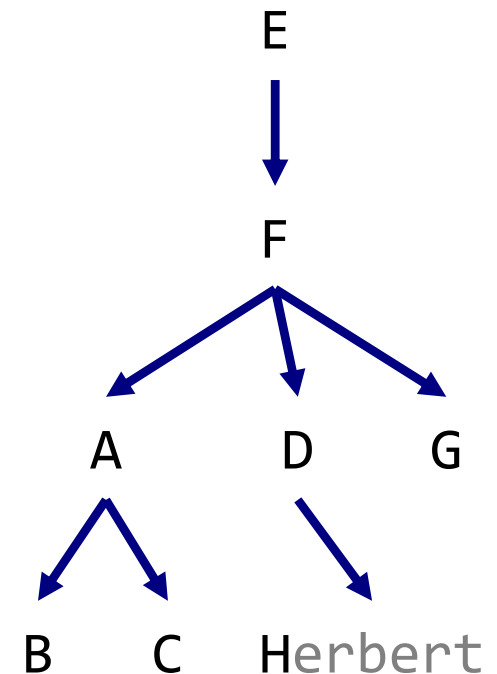
```
logic> (query (child ?child fillmore))
```

Success!

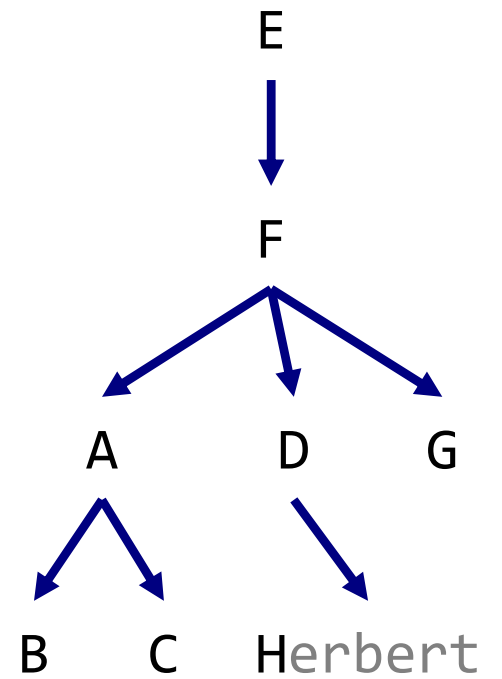
child: abraham

child: delano

child: grover



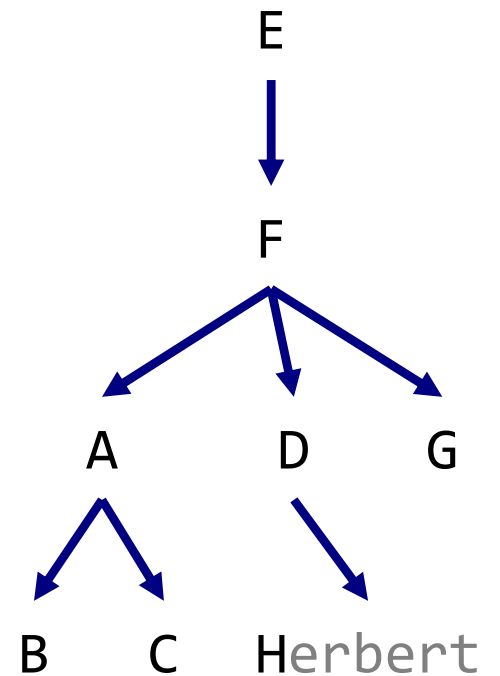
# Recursive Facts



# Recursive Facts



A fact is recursive if the same relation is mentioned in a hypothesis and the conclusion



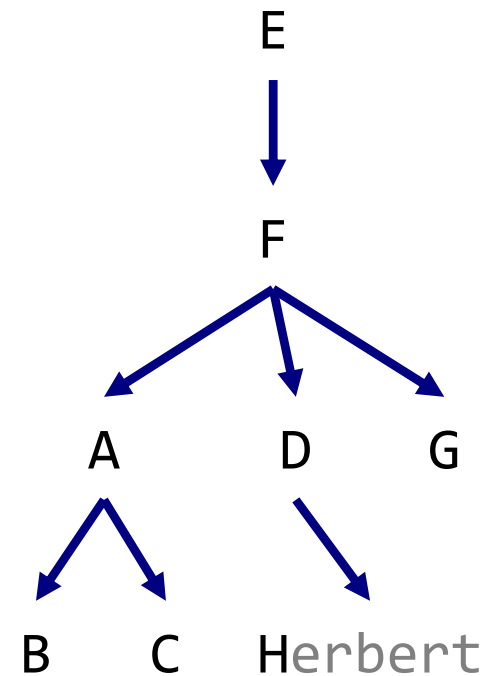
# Recursive Facts



A fact is recursive if the same relation is mentioned in a hypothesis and the conclusion

```
logic> (fact (ancestor ?a ?y) (parent ?a ?y))
```

```
logic> (fact (ancestor ?a ?y) (parent ?a ?z) (ancestor ?z ?y))
```





# Recursive Facts



A fact is recursive if the same relation is mentioned in a hypothesis and the conclusion

```
logic> (fact (ancestor ?a ?y) (parent ?a ?y))
```

```
logic> (fact (ancestor ?a ?y) (parent ?a ?z) (ancestor ?z ?y))
```

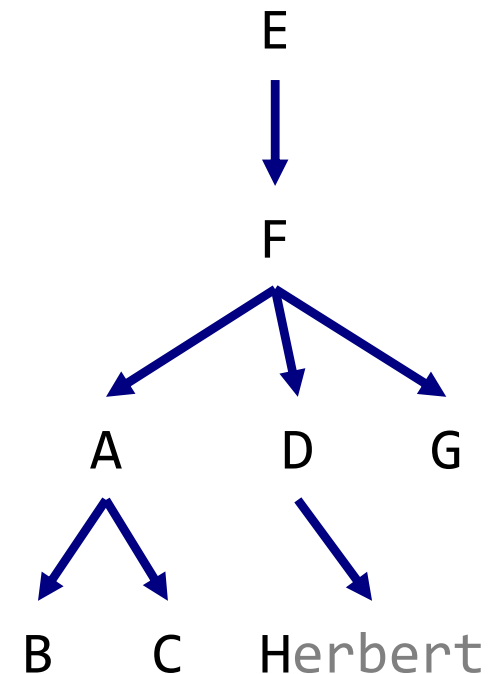
```
logic> (query (ancestor ?a herbert))
```

Success!

a: delano

a: fillmore

a: eisenhower



# Recursive Facts



A fact is recursive if the same relation is mentioned in a hypothesis and the conclusion

```
logic> (fact (ancestor ?a ?y) (parent ?a ?y))
```

```
logic> (fact (ancestor ?a ?y) (parent ?a ?z) (ancestor ?z ?y))
```

```
logic> (query (ancestor ?a herbert))
```

Success!

a: delano

a: fillmore

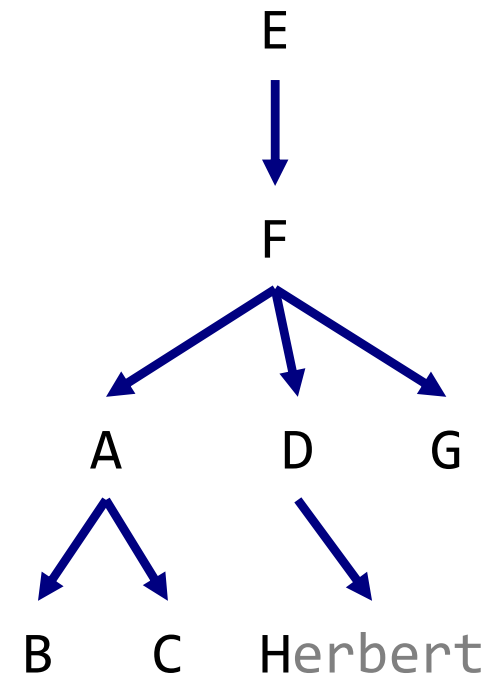
a: eisenhower

```
logic> (query (ancestor ?a barack)
            (ancestor ?a herbert))
```

Success!

a: fillmore

a: eisenhower



# Searching to Satisfy Queries

---



# Searching to Satisfy Queries



The *Logic* interpreter performs a search in the space of relations for each query to find a satisfying assignment

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logic> (query (ancestor ?a herbert))
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```
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```

```
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```

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```

```
a: eisenhower
```

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The *Logic* interpreter performs a search in the space of relations for each query to find a satisfying assignment

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```

```
Success!
```

```
a: delano
```

```
a: fillmore
```



```
a: eisenhower
```

# Searching to Satisfy Queries



The *Logic* interpreter performs a search in the space of relations for each query to find a satisfying assignment

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logic> (query (ancestor ?a herbert))
```

```
Success!
```

```
a: delano
```

```
a: fillmore ←
```

```
a: eisenhower
```

```
logic> (fact (parent delano herbert))
```

```
logic> (fact (parent fillmore delano))
```

# Searching to Satisfy Queries



The *Logic* interpreter performs a search in the space of relations for each query to find a satisfying assignment

```
logic> (query (ancestor ?a herbert))
```

Success!

a: delano

a: fillmore 

a: eisenhower

```
logic> (fact (parent delano herbert))
```

```
logic> (fact (parent fillmore delano))
```

```
logic> (fact (ancestor ?a ?y) (parent ?a ?y))
```

```
logic> (fact (ancestor ?a ?y) (parent ?a ?z) (ancestor ?z ?y))
```



# Searching to Satisfy Queries



The *Logic* interpreter performs a search in the space of relations for each query to find a satisfying assignment

```
logic> (query (ancestor ?a herbert))
```

```
Success!
```

```
a: delano
```

```
a: fillmore ←
```

```
a: eisenhower
```

```
logic> (fact (parent delano herbert))
```

```
logic> (fact (parent fillmore delano))
```

```
logic> (fact (ancestor ?a ?y) (parent ?a ?y))
```

```
logic> (fact (ancestor ?a ?y) (parent ?a ?z) (ancestor ?z ?y))
```

```
(parent delano herbert) ; (1), a simple fact
```

# Searching to Satisfy Queries



The *Logic* interpreter performs a search in the space of relations for each query to find a satisfying assignment

```
logic> (query (ancestor ?a herbert))
```

Success!

a: delano

a: fillmore



a: eisenhower

```
logic> (fact (parent delano herbert))
```

```
logic> (fact (parent fillmore delano))
```

```
logic> (fact (ancestor ?a ?y) (parent ?a ?y))
```

```
logic> (fact (ancestor ?a ?y) (parent ?a ?z) (ancestor ?z ?y))
```

(parent delano herbert) ; (1), a simple fact

(ancestor delano herbert) ; (2), from (1) and the 1st ancestor fact

# Searching to Satisfy Queries



The *Logic* interpreter performs a search in the space of relations for each query to find a satisfying assignment

```
logic> (query (ancestor ?a herbert))
```

Success!

a: delano

a: fillmore



a: eisenhower

```
logic> (fact (parent delano herbert))
```

```
logic> (fact (parent fillmore delano))
```

```
logic> (fact (ancestor ?a ?y) (parent ?a ?y))
```

```
logic> (fact (ancestor ?a ?y) (parent ?a ?z) (ancestor ?z ?y))
```

(parent delano herbert) ; (1), a simple fact

(ancestor delano herbert) ; (2), from (1) and the 1st ancestor fact

(parent fillmore delano) ; (3), a simple fact

# Searching to Satisfy Queries



The *Logic* interpreter performs a search in the space of relations for each query to find a satisfying assignment

```
logic> (query (ancestor ?a herbert))
```

Success!

a: delano

a: fillmore



a: eisenhower

```
logic> (fact (parent delano herbert))
```

```
logic> (fact (parent fillmore delano))
```

```
logic> (fact (ancestor ?a ?y) (parent ?a ?y))
```

```
logic> (fact (ancestor ?a ?y) (parent ?a ?z) (ancestor ?z ?y))
```

(parent delano herbert) ; (1), a simple fact

(ancestor delano herbert) ; (2), from (1) and the 1st ancestor fact

(parent fillmore delano) ; (3), a simple fact

(ancestor fillmore herbert) ; (4), from (2), (3), & the 2nd ancestor fact

# Hierarchical Facts



# Hierarchical Facts



Relations can contain relations in addition to atoms

# Hierarchical Facts



Relations can contain relations in addition to atoms

```
logic> (fact (dog (name abraham) (color white)))
```

# Hierarchical Facts



Relations can contain relations in addition to atoms

```
logic> (fact (dog (name abraham) (color white)))  
logic> (fact (dog (name barack) (color tan)))  
logic> (fact (dog (name clinton) (color white)))  
logic> (fact (dog (name delano) (color white)))  
logic> (fact (dog (name eisenhower) (color tan)))  
logic> (fact (dog (name fillmore) (color brown)))  
logic> (fact (dog (name grover) (color tan)))  
logic> (fact (dog (name herbert) (color brown)))
```

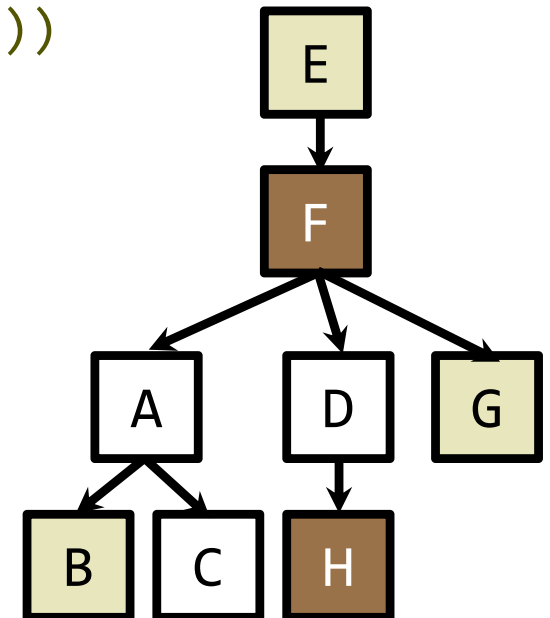


# Hierarchical Facts



Relations can contain relations in addition to atoms

```
logic> (fact (dog (name abraham) (color white)))  
logic> (fact (dog (name barack) (color tan)))  
logic> (fact (dog (name clinton) (color white)))  
logic> (fact (dog (name delano) (color white)))  
logic> (fact (dog (name eisenhower) (color tan)))  
logic> (fact (dog (name fillmore) (color brown)))  
logic> (fact (dog (name grover) (color tan)))  
logic> (fact (dog (name herbert) (color brown)))
```



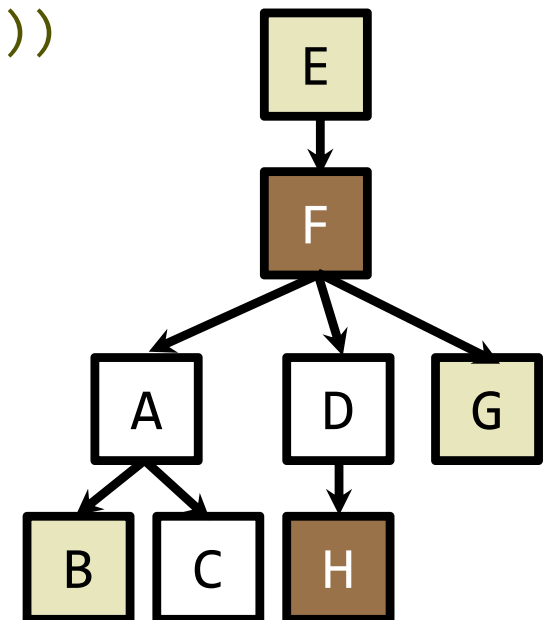
# Hierarchical Facts



Relations can contain relations in addition to atoms

```
logic> (fact (dog (name abraham) (color white)))  
logic> (fact (dog (name barack) (color tan)))  
logic> (fact (dog (name clinton) (color white)))  
logic> (fact (dog (name delano) (color white)))  
logic> (fact (dog (name eisenhower) (color tan)))  
logic> (fact (dog (name fillmore) (color brown)))  
logic> (fact (dog (name grover) (color tan)))  
logic> (fact (dog (name herbert) (color brown)))
```

Variables can refer to atoms or relations



# Hierarchical Facts

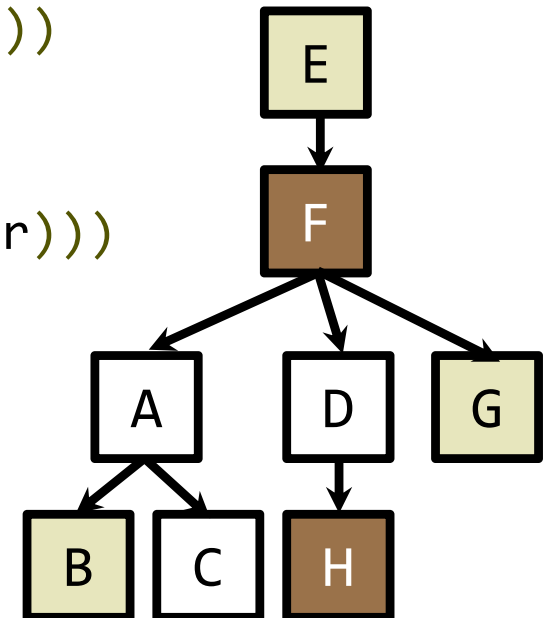


Relations can contain relations in addition to atoms

```
logic> (fact (dog (name abraham) (color white)))  
logic> (fact (dog (name barack) (color tan)))  
logic> (fact (dog (name clinton) (color white)))  
logic> (fact (dog (name delano) (color white)))  
logic> (fact (dog (name eisenhower) (color tan)))  
logic> (fact (dog (name fillmore) (color brown)))  
logic> (fact (dog (name grover) (color tan)))  
logic> (fact (dog (name herbert) (color brown)))
```

Variables can refer to atoms or relations

```
logic> (query (dog (name clinton) (color ?color)))  
Success!  
color: white
```



# Hierarchical Facts

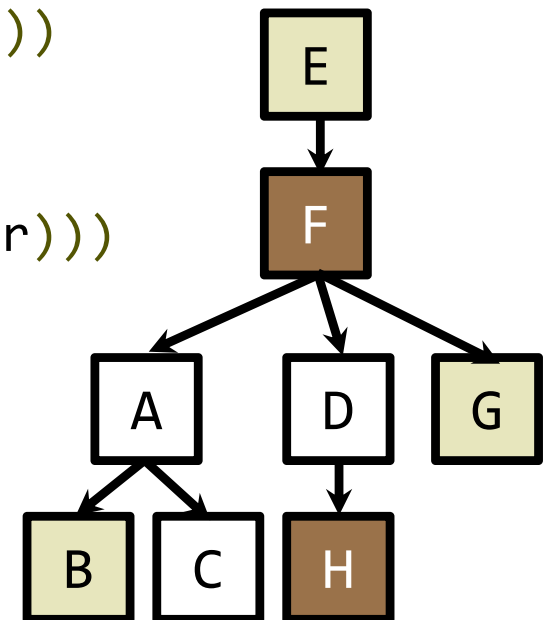


Relations can contain relations in addition to atoms

```
logic> (fact (dog (name abraham) (color white)))  
logic> (fact (dog (name barack) (color tan)))  
logic> (fact (dog (name clinton) (color white)))  
logic> (fact (dog (name delano) (color white)))  
logic> (fact (dog (name eisenhower) (color tan)))  
logic> (fact (dog (name fillmore) (color brown)))  
logic> (fact (dog (name grover) (color tan)))  
logic> (fact (dog (name herbert) (color brown)))
```

Variables can refer to atoms or relations

```
logic> (query (dog (name clinton) (color ?color)))  
Success!  
color: white  
  
logic> (query (dog (name clinton) ?info))  
Success!  
info: (color white)
```



# Hierarchical Facts

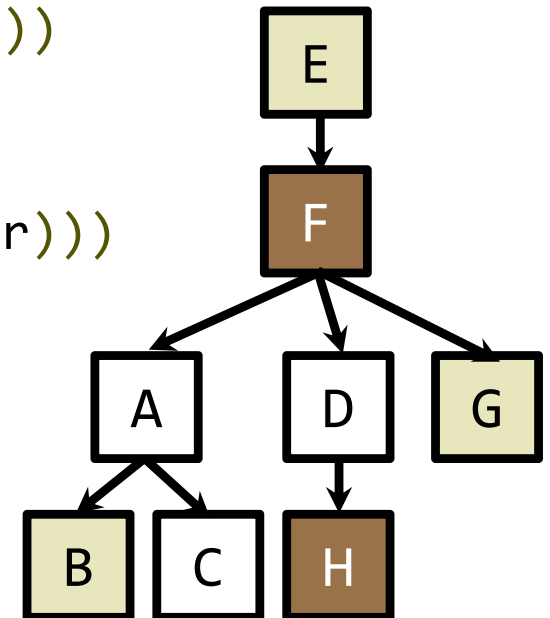


Relations can contain relations in addition to atoms

```
logic> (fact (dog (name abraham) (color white)))  
logic> (fact (dog (name barack) (color tan)))  
logic> (fact (dog (name clinton) (color white)))  
logic> (fact (dog (name delano) (color white)))  
logic> (fact (dog (name eisenhower) (color tan)))  
logic> (fact (dog (name fillmore) (color brown)))  
logic> (fact (dog (name grover) (color tan)))  
logic> (fact (dog (name herbert) (color brown)))
```

Variables can refer to atoms or relations

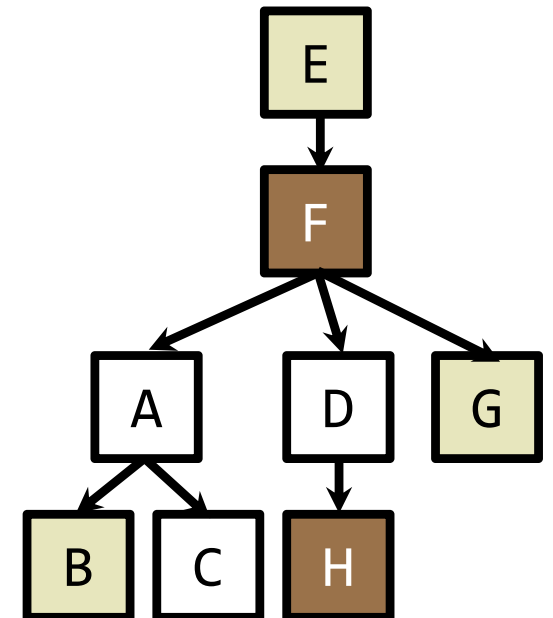
```
logic> (query (dog (name clinton) (color ?color)))  
Success!  
color: white  
  
logic> (query (dog (name clinton) ?info))  
Success!  
info: (color white)
```



# Example: Combining Multiple Data Sources



Which dogs have an ancestor of the same color?

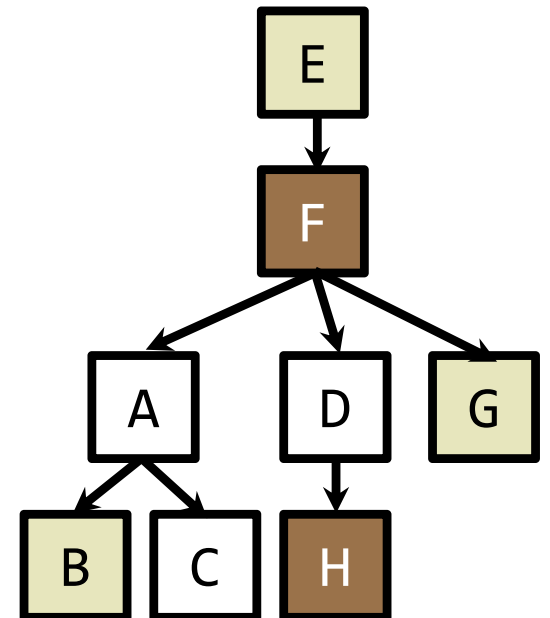


# Example: Combining Multiple Data Sources



Which dogs have an ancestor of the same color?

```
logic> (query (dog (name ?name) (color ?color)))
```

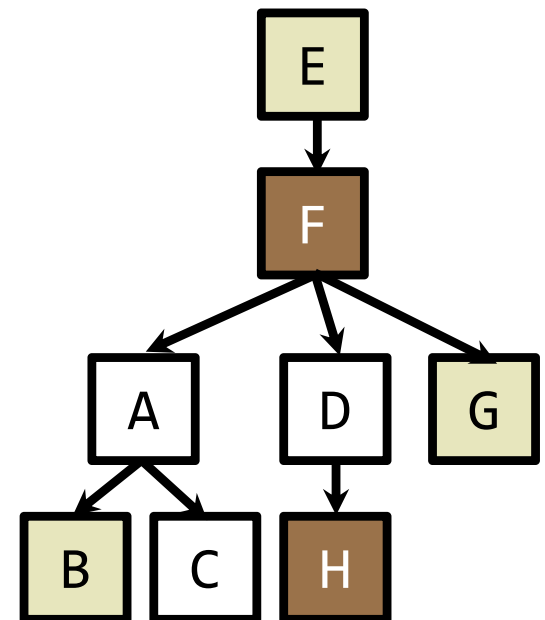


# Example: Combining Multiple Data Sources



Which dogs have an ancestor of the same color?

```
logic> (query (dog (name ?name) (color ?color))  
           (ancestor ?ancestor ?name))
```



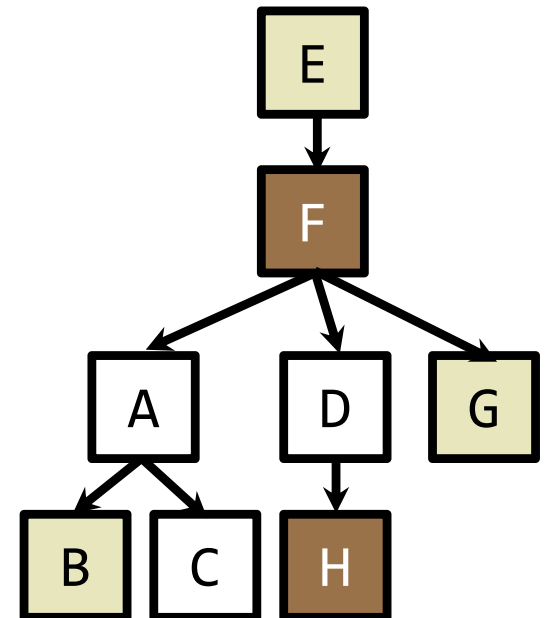


# Example: Combining Multiple Data Sources



Which dogs have an ancestor of the same color?

```
logic> (query (dog (name ?name) (color ?color))  
            (ancestor ?ancestor ?name)  
            (dog (name ?ancestor) (color ?color))))
```



# Example: Combining Multiple Data Sources

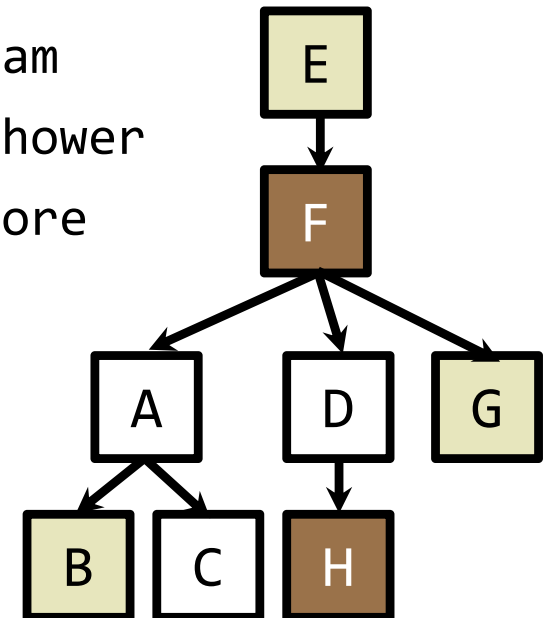


Which dogs have an ancestor of the same color?

```
logic> (query (dog (name ?name) (color ?color))  
           (ancestor ?ancestor ?name)  
           (dog (name ?ancestor) (color ?color)))
```

Success!

name: barack	color: tan	ancestor: eisenhower
name: clinton	color: white	ancestor: abraham
name: grover	color: tan	ancestor: eisenhower
name: herbert	color: brown	ancestor: fillmore



# Example: Appending Lists



# Example: Appending Lists



Two lists append to form a third list if:

# Example: Appending Lists



Two lists append to form a third list if:

- The first list is empty and the second and third are the same

# Example: Appending Lists



Two lists append to form a third list if:

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( ) (a b c) (a b c)

# Example: Appending Lists



Two lists append to form a third list if:

- The first list is empty and the second and third are the same

`() (a b c) (a b c)`

```
logic> (fact (append-to-form () ?x ?x))
```

# Example: Appending Lists



Two lists append to form a third list if:

- The first list is empty and the second and third are the same

`() (a b c) (a b c)`

- Both of the following hold:

```
logic> (fact (append-to-form () ?x ?x))
```



# Example: Appending Lists



Two lists append to form a third list if:

- The first list is empty and the second and third are the same

`() (a b c) (a b c)`

- Both of the following hold:
  - List 1 and 3 have the same first element

```
logic> (fact (append-to-form () ?x ?x))
```

# Example: Appending Lists



Two lists append to form a third list if:

- The first list is empty and the second and third are the same

`() (a b c) (a b c)`

- Both of the following hold:
  - List 1 and 3 have the same first element

`(a b c) (d e f) (a b c d e f)`

```
logic> (fact (append-to-form () ?x ?x))
```

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Two lists append to form a third list if:

- The first list is empty and the second and third are the same

`() (a b c) (a b c)`

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```
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- The first list is empty and the second and third are the same

`() (a b c) (a b c)`

- Both of the following hold:
  - List 1 and 3 have the same first element

`(a b c) (d e f) (a b c d e f)`

```
logic> (fact (append-to-form () ?x ?x))
```

```
logic> (fact (append-to-form (?a . ?r) ?y (?a . ?z)))
```

# Example: Appending Lists



Two lists append to form a third list if:

- The first list is empty and the second and third are the same

`() (a b c) (a b c)`

- Both of the following hold:

- List 1 and 3 have the same first element
- The rest of list 1 and all of list 2 append to form the rest of list 3

`(a b c) (d e f) (a b c d e f)`

```
logic> (fact (append-to-form () ?x ?x))
```

```
logic> (fact (append-to-form (?a . ?r) ?y (?a . ?z)))
```

# Example: Appending Lists



Two lists append to form a third list if:

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`() (a b c) (a b c)`

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logic> (fact (append-to-form () ?x ?x))
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logic> (fact (append-to-form (?a . ?r) ?y (?a . ?z)))
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# Example: Appending Lists



Two lists append to form a third list if:

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- The rest of list 1 and all of list 2 append to form the rest of list 3

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logic> (fact (append-to-form () ?x ?x))
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logic> (fact (append-to-form (?a . ?r) ?y (?a . ?z)))
```



# Example: Appending Lists



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`() (a b c) (a b c)`

- Both of the following hold:
  - List 1 and 3 have the same first element
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logic> (fact (append-to-form () ?x ?x))
```

```
logic> (fact (append-to-form (?a . ?r) ?y (?a . ?z)))
```

# Example: Appending Lists



Two lists append to form a third list if:

- The first list is empty and the second and third are the same

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- Both of the following hold:
  - List 1 and 3 have the same first element
  - The rest of list 1 and all of list 2 append to form the rest of list 3

`(a b c) (d e f) (a b c d e f)`

```
logic> (fact (append-to-form () ?x ?x))
```

```
logic> (fact (append-to-form (?a . ?r) ?y (?a . ?z))  
          (append-to-form ?r ?y ?z))
```